# Package 'CUSUMdesign' 

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Type Package
Title Compute Decision Interval and Average Run Length for CUSUM Charts
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## Description

Computation of decision intervals (H) and average run lengths (ARL) for CUSUM charts. Details of the method are seen in Hawkins and Olwell (2012): Cumulative sum charts and charting for quality improvement, Springer Science \& Business Media.
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$\qquad$
getARL compute average run length (ARL) for CUSUM charts

## Description

Compute average run lengths for CUSUM charts based on the Markov chain algorithm.

## Usage

getARL(distr=NULL, K=NULL, H=NULL, Mean=NULL, std=NULL, prob=NULL, Var=NULL, mu=NULL, lambda=NULL, samp.size=NULL, is.upward=NULL, winsrl=NULL, winsru=NULL)

## Arguments

distr Integer valued from 1 to 6: 1 refers to "normal mean", 2 refers to "normal variance", 3 refers to "Poisson", 4 refers to "binomial", 5 refers to "negative binomial", and 6 refers to "inverse Gaussian mean".
K A reference value, which is given by geth.
H A given decision interval, which is given by getH.
Mean Mean value, which has to be provided when distr $=1$ (normal mean), 3 (Poisson), and 5 (negative binomial). The value must be positive when distr $=3$ or distr $=5$.
std Standard deviation, which has to be provided when distr $=1$ (normal mean) and 2 (normal variance). The value must be positive.
prob $\quad$ Success probability, which has to be provided when distr $=4$ (binomial); $0<$ prob $<=1$.
Var Variance, which has to be provided when distr $=5$ (negative binomial). The value has to be larger than Mean when distr $=5$.
mu A positive value representing the mean of inverse Gaussian distribution. The argument 'mu' has to be provided when distr $=6$ (inverse Gaussian mean).
lambda A positive value representing the shape parameter for inverse Gaussian distribution. The argument 'lambda' has to be provided when distr $=6$ (inverse Gaussian mean).
samp.size Sample size, an integer which has to be provided when distr $=2$ (normal variance) or distr $=4$ (binomial).
is.upward Logical value, whether to depict a upward or downward CUSUM.
winsrl Lower Winsorizing constant. Use NULL or -999 if Winsorization is not needed.
winsru Upper Winsorizing constant. Use NULL or 999 if Winsorization is not needed.

## Details

Computes ARL when the reference value and decision interval are given. For each case, the necessary parameters are listed as follows.

Normal mean (distr $=1$ ): Mean, std, K, H.
Normal variance (distr = 2): samp. size, std, K, H.
Poisson (distr = 3): Mean, K, H.
Binomial (dist = 4): samp. size, prob, K, H.
Negative binomial (distr = 5): Mean, Var, K, H.
Inverse Gaussian mean $(\operatorname{distr}=6)$ : mu, lambda, $\mathrm{K}, \mathrm{H}$.

## Value

A list including three variables:

ARL_Z The computed zero-start average run length for CUSUM.
ARL_F The computed fast-initial-response (FIR) average run length for CUSUM.
ARL_S The computed steady-state average run length for CUSUM.

## Author(s)

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## References

Hawkins, D. M. and Olwell, D. H. (1998) 'Cumulative Sum Charts and Charting for Quality Improvement (Information Science and Statistics)", Springer, New York.

## See Also

```
getH
```


## Examples

```
# normal mean
getARL(distr=1, K=11, H=5, Mean=10, std=2)
# normal variance
getARL(distr=2, K=3, H=1, std=2, samp.size=5, is.upward=TRUE)
# Poission
getARL(distr=3, K=3, H=1, std=2, Mean=5, is.upward=TRUE)
# Binomial
getARL(distr=4, K=0.8, H=1, prob=0.2, samp.size=100, is.upward=TRUE)
# Negative binomial
getARL(distr=5, K=3, H=6, Mean=2, Var=5, is.upward=TRUE)
# Inverse Gaussian mean
getARL(distr=6, K=2, H=4, mu=3, lambda=0.5, is.upward=TRUE)
```


## Description

Compute decision intervals for CUSUM charts.

## Usage

getH(distr=NULL, ARL=NULL, ICmean=NULL, ICsd=NULL,
OOCmean=NULL, OOCsd=NULL, ICprob=NULL, OOCprob=NULL,
ICvar=NULL, IClambda=NULL, samp.size=NULL,
ref=NULL, winsrl=NULL, winsru=NULL,
type=c("fast initial response", "zero start", "steady state"))

## Arguments

distr Integer valued from 1 to 6: 1 refers to "normal mean", 2 refers to "normal variance", 3 refers to "Poisson", 4 refers to "binomial", 5 refers to "negative binomial", 6 refers to "inverse Gaussian mean".
ARL An integer for in control average run length.
ICmean In-control mean, which has to be provided when distr $=1$ (normal mean), 3 (Poisson), 5 (negative binomial), and 6 (inverse Gaussian mean). The value has to be positive when distr $=3$, distr $=5$, or distr $=6$.
ICsd In-control standard deviation, which has to be provided when distr $=1$ (normal mean) and 2 (normal variance). The value has to be positive.

00Cmean Out-of-control mean, which has to be provided when distr $=1$ (normal mean), 3 (Poisson), 5 (negative binomial), and 6 (Inverse Gaussian mean). When distr $=$ 3,5 , or 6 , the value has to be positive.
OOCsd Out-of-control standard deviation, which has to be provided when distr $=2$ (normal variance). The value has to be positive.
ICprob In-control success probability, which has to be provided when distr $=4$ (binomial); $0<$ prob $<=1$.
OOCprob Out-of-control success probability, which has to be provided when distr $=4$ (binomial); $0<$ prob $<=1$.
ICvar In-control variance, which has to be provided when distr $=5$ (negative binomial). The value has to be larger than the in-control mean 'ICmean'.
IClambda In-control shape parameter for inverse Gaussian distribution. The argument 'IClambda' has to be provided when distr $=6$ (inverse Gaussian mean).
samp.size Sample size, an integer which has to be provided when distr = 2 (normal variance) or distr $=4$ (binomial).
ref Optional reference value.
winsrl Lower Winsorizing constant. Use NULL or -999 if Winsorization is not needed.
winsru Upper Winsorizing constant. Use NULL or 999 if Winsorization is not needed.
type
A string for CUSUM type: "F" for fast-initial-response CUSUM, "Z" for zerostart CUSUM, and "S" for steady-state CUSUM. Default is "F".

## Details

Computes the decision interval H when the reference value and the average run length are given. For each case, the necessary parameters are listed as follows.

Normal mean (distr = 1): ICmean, ICsd, 00Cmean.
Normal variance (distr = 2): samp. size, ICsd, OOCsd
Poisson (distr = 3): ICmean, 00Cmean.
Binomial (dist = 4): samp. size, ICprob, 00Cprob.
Negative binomial (distr = 5): ICmean, Icvar, 00Cmean.
Inverse Gaussian mean (distr $=6$ ): ICmean, IClambda, 00Cmean.

## Value

A list including three variables:
DI Decision interval.
IC_ARL In-control average run length.
OOCARL_Z Out-of-control average run length for the zero-start CUSUM.
OOCARL_F Out-of-control average run length for the fast-initial-response (FIR) CUSUM.
OOCARL_S Out-of-control average run length for the steady-state CUSUM.

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## References

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## See Also

getARL

## Examples

```
# normal mean
getH(distr=1, ICmean=10, ICsd=2, 00Cmean=15, ARL=1000, type="F")
# normal variance
getH(distr=2, ICsd=2, OOCsd=4, samp.size=5, ARL=1000, type="F")
```

```
# Poission
getH(distr=3, ICmean=2, 00Cmean=3, ARL=100, type="F")
# Binomial
getH(distr=4, ICprob=0.2, OOCprob=0.6, samp.size=100, ARL=1000, type="F")
# Negative binomial
getH(distr=5, ICmean=1, ICvar=3, 00Cmean=2, ARL=100, type="F")
# Inverse Gaussian mean
getH(distr=6, ICmean=1, IClambda=0.5, O0Cmean=2, ARL=1000, type="F")
```


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