# Package 'MAINT.Data'

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Author Pedro Duarte Silva <psilva@ucp.pt>, Paula Brito <mpbrito.fep.up.pt></mpbrito.fep.up.pt></psilva@ucp.pt>
Maintainer Pedro Duarte Silva <psilva@ucp.pt></psilva@ucp.pt>
Description Implements methodologies for modelling interval data by Normal and Skew-Normal distributions, considering appropriate parameterizations of the variance-covariance matrix that takes into account the intrinsic nature of interval data, and lead to four different possible configuration structures.  The Skew-Normal parameters can be estimated by maximum likelihood, while Normal parameters may be estimated by maximum likelihood or robust trimmed maximum likelihood methods.
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MAIN	.Data-package Modelling and Analizing Interval Data	

# Description

MAINT.Data implements methodologies for modelling Interval Data by Normal and Skew-Normal distributions, considering four different possible configurations structures for the variance-covariance matrix. It introduces a data class for representing interval data and includes functions and methods for parametric modelling and analysing of interval data. It performs maximum likelihood and trimmed maximum likelihood estimation, statistical tests, as well as (M)ANOVA, Discriminant Analysis and Gaussian Model Based Clustering.

# Details

In the classical model of multivariate data analysis, data is represented in a data-array where n "individuals" (usually in rows) take exactly one value for each variable (usually in columns). Symbolic Data Analysis (see, e.g., Noirhomme-Fraiture and Brito (2011)) provides a framework where new variable types allow to take directly into account variability and/or uncertainty associated to each single "individual", by allowing multiple, possibly weighted, values for each variable. New variable types - interval, categorical multi-valued and modal variables - have been introduced.

We focus on the analysis of interval data, i.e., where elements are described by variables whose values are intervals. Parametric inference methodologies based on probabilistic models for interval variables are developed in Brito and Duarte Silva (2011) where each interval is represented by its midpoint and log-range, for which Normal and Skew-Normal (Azzalini and Dalla Valle (1996)) distributions are assumed. The intrinsic nature of the interval variables leads to special structures of the variance-covariance matrix, which are represented by four different possible configurations.

MAINT.Data implements the proposed methodologies in R, introducing a data class for representing interval data; it includes functions for modelling and analysing interval data, in particular maximum likelihood and trimmed maximum likelihood (Duarte Silva, Filzmoser and Brito (2017)) estimation, and statistical tests for the different considered configurations. Methods for (M)ANOVA, Discriminant Analysis (Duarte Silva and Brito (2015)) and model based clustering (Brito, Duarte Silva and Dias (2015)) of this data class are also provided.

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## Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

Maintainer: Pedro Duarte Silva <psilva@porto.ucp.pt>

#### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P. and Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Brito, P., Duarte Silva, A. P. and Dias, J. G. (2015), Probabilistic Clustering of Interval Data. *Intelligent Data Analysis* **19**(2), 293–313.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Noirhomme-Fraiture, M. and Brito, P. (2011), Far Beyond the Classical Data Models: Symbolic Data Analysis. *Statistical Analysis and Data Mining* **4**(2), 157–170.

# **Examples**

- # Create an Interval-Data object containing the intervals for 899 observations
- $\mbox{\#}$  on the temperatures by quarter in 60 Chinese meteorological stations.

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```
ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))</pre>
#Display the first and last observations
head(ChinaT)
tail(ChinaT)
#Print summary statistics
summary(ChinaT)
#Create a new data set considering only the Winter (1st and 4th) quarter intervals
ChinaWT <- ChinaT[,c(1,4)]</pre>
# Estimate normal distribution parameters by maximum likelihood, assuming
# the classical (unrestricted) covariance configuration Case 1
ChinaWTE.C1 <- mle(ChinaWT,CovCase=1)</pre>
cat("Winter temperatures of China -- normal maximum likelhiood estimation results:\n")
print(ChinaWTE.C1)
cat("Standard Errors of Estimators:\n") ; print(stdEr(ChinaWTE.C1))
# Estimate normal distribution parameters by maximum likelihood,
# assuming that one of the C2, C3 or C4 restricted covariance configuration cases hold
ChinaWTE.C234 <- mle(ChinaWT,CovCase=2:4)
cat("Winter temperatures of China -- normal maximum likelihood estimation results:\n")
print(ChinaWTE.C234)
cat("Standard Errors of Estimators:\n") ; print(stdEr(ChinaWTE.C234))
# Estimate normal distribution parameters robustly by fast maximun trimmed likelihood,
# assuming that one of the C2, C3 or C4 restricted covariance configuration cases hold
## Not run:
ChinaWTE.C234 <- fasttle(ChinaWT,CovCase=2:4)</pre>
cat("Winter temperatures of China -- normal maximum trimmed likelhiood estimation results:\n")
print(ChinaWTE.C234)
# Estimate skew-normal distribution parameters
ChinaWTE.SkN <- mle(ChinaWT, Model="SKNormal")</pre>
cat("Winter temperatures of China -- Skew-Normal maximum likelhiood estimation results:\n")
print(ChinaWTE.SkN)
cat("Standard Errors of Estimators:\n") ; print(stdEr(ChinaWTE.SkN))
## End(Not run)
#MANOVA tests assuming that configuration case 1 (unrestricted covariance)
# or 3 (MidPoints independent of Log-Ranges) holds.
ManvChinaWT.C13 <- MANOVA(ChinaWT,ChinaTemp$GeoReg,CovCase=c(1,3))</pre>
```

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```
cat("Winter temperatures of China -- MANOVA by geografical regions results:\n")
print(ManvChinaWT.C13)
#Linear Discriminant Analysis
ChinaWT.lda <- lda(ManvChinaWT.C13)</pre>
cat("Winter temperatures of China -- linear discriminant analysis results:\n")
print(ChinaWT.lda)
cat("lda Prediction results:\n")
print(predict(ChinaWT.lda,ChinaWT)$class)
## Not run:
#Estimate error rates by ten-fold cross-validation
CVlda <- DACrossVal(ChinaWT, ChinaTemp$GeoReg, TrainAlg=lda,
CovCase=BestModel(H1res(ManvChinaWT.C13)),CVrep=1)
#Robust Quadratic Discriminant Analysis
ChinaWT.rqda <- Robqda(ChinaWT,ChinaTemp$GeoReg)</pre>
cat("Winter temperatures of China -- robust quadratic discriminant analysis results:\n")
print(ChinaWT.rqda)
cat("robust qda prediction results:\n")
print(predict(ChinaWT.rqda,ChinaWT)$class)
## End(Not run)
# Create an Interval-Data object containing the intervals of loan data
# (from the Kaggle Data Science platform) aggregated by loan purpose
LbyPIdt <- IData(LoansbyPurpose_minmaxDt,</pre>
  VarNames=c("ln-inc","ln-revolbal","open-acc","total-acc"))
print(LbyPIdt)
## Not run:
#Fit homoscedastic Gaussian mixtures with up to six components
mclustres <- Idtmclust(LbyPIdt,G=1:6)</pre>
plotInfCrt(mclustres,legpos="bottomright")
print(mclustres)
#Display the results of the best mixture according to the BIC
summary(mclustres,parameters=TRUE,classification=TRUE)
pcoordplot(mclustres)
## End(Not run)
```

Abalone 7

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## **Description**

A interval-valued data set containing 24 units, created from from the Abalone dataset (UCI Machine Learning Repository), after aggregating by sex and age.

## Usage

```
data(Abalone)
```

## **Format**

AbdaDF: A data frame containing the original 4177 Abalone individuals described by 7 variables. AbUnits: A factor with 4177 observations and 24 levels indicating the sex by age combination to which each orginal individual belongs to.

AbaloneIdt: An IData object with 24 observations and 7 interval-valued variables, describing the intervals formed by aggregating the AbdaDF microdata by the AbUnits factor.

# **Description**

AgrMcDt creates IData objects by agregating a Data Frame of Micro Data.

# Usage

```
AgrMcDt(MicDtDF, agrby, agrcrt="minmax")
```

## **Arguments**

MicDtDF	A data frame with the original values of the micro data.
agrby	A factor with categories on which the micro data should be aggregated.
agrcrt	The aggregation criterion. Either the 'minmax' string, or a two dimensional vector with the prob. value for the left (lower) percentile, followed by the prob.

value for the right (upper) percentile, used in the aggregation.

# Value

An object of class IData with the data set of Interval-valued variables resulting from the aggregation performed.

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## See Also

**IData** 

# Examples

```
# Create an Interval-Data object by agregating the microdata consisting
# of 336776 NYC flights included in the FlightsDF data frame,
# by the statistical units specified in the FlightsUnits factor.
Flightsminmax <- AgrMcDt(FlightsDF,FlightsUnits)</pre>
#Display the first and last observations
head(Flightsminmax)
tail(Flightsminmax)
#Print summary statistics
summary(Flightsminmax)
## Not run:
# Repeat this procedure using now the 10th and 90th percentiles.
Flights1090prcnt <- AgrMcDt(FlightsDF,FlightsUnits,agrcrt=c(0.1,0.9))</pre>
#Display the first and last observations
head(Flights1090prcnt)
tail(Flights1090prcnt)
summary(Flights1090prcnt)
## End(Not run)
```

BestModel-methods

Methods for function BestModel in Package 'MAINT.Data'

# **Description**

Selects the best model according to the chosen selection criterion (currently, BIC or AIC)

# Usage

```
BestModel(ModE,SelCrit=c("IdtCrt","BIC","AIC"))
```

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## **Arguments**

ModE An object of class IdtE representing the estimates of a model fitted to a data set

of interval-value variables

SelCrit The model selection criterion. "IdtCrt" stands for the criterion originally used in

the ModE estimation, while "BIC" and "AIC" represent respectively the Bayesian

and Akaike information criteria.

#### Value

An integer with the index of the model chosen by the selection criterion

Cars Data Set

# Description

This data set consist of the intervals for four characteristics (Price, EngineCapacity, TopSpeed and Acceleration) of 27 cars models partitioned into four different classes (Utilitarian, Berlina, Sportive and Luxury).

## Usage

data(Cars)

## **Format**

A data frame containing 27 observations on 9 variables, the first eight with the lower and upper bounds of the interval characteristics for 27 car models, the last one a factor indicating the model class.

ChinaTemperatures Data Set

# **Description**

This data set consist of the intervals of observed temperatures (Celsius scale) in each of the four quarters, Q\_1 to Q\_4, of the years 1974 to 1988 in 60 chinese meteorologic stations; one outlier observation (YinChuan\_1982) has been discarded. The 60 stations belong to different regions in China, which therefore define a partition of the 899 stations-year combinations.

# Usage

data(ChinaTemp)

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#### **Format**

A data frame containing 899 observations on 9 variables, the first eight with the lower and upper bounds of the temperatures by quarter in the 899 stations-year combinations, the last one a factor indicating the geographic region of each station.

coef--methods

Methods for function coef in Package 'MAINT.Data'

## **Description**

S4 methods for function coef. As in the generic coef S3 'stats' method, these methods extract parameter estimates for the models fitted to Interval Data.

# Usage

```
## S4 method for signature 'IdtNDE'
coef(object, selmodel=BestModel(object), ...)
## S4 method for signature 'IdtSNDE'
coef(object, selmodel=BestModel(object), ParType=c("Centr", "Direct", "All"), ...)
## S4 method for signature 'IdtNandSNDE'
coef(object, selmodel=BestModel(object), ParType=c("Centr", "Direct", "All"), ...)
```

#### **Arguments**

object An object representing a model fitted to interval data.

selmodel Selected model from a list of candidate models saved in object.

ParType Parameterization of the Skew-Normal distribution. Only used when object has

class IdtSNDE or IdtNandSNDE and in this latter case when argument "selmodel"

chooses a Skew-Normal model.

Alternatives are "Centr" for centred parameters, "Direct" for direct parameters and "All", for both types of parameters. See Arellano-Valle and Azzalini (2008)

for details.

... Additional arguments for method functions.

#### Value

A list of parameter estimates. The list components depend on the model and parametriztion assumed by the model. For Gaussian models these are respectively mu (vector of mean estimates) and Sigma (matrix of covariance estimates). For Skew-Normal models the components are mu, Sigma and gamma1 (one vector of skewness coefficient estimates) for the centred parametrization and the vectors ksi, and alpha, and the matrix Omega for the direct parametrization.

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## References

Arellano-Valle, R. B. and Azzalini, A. (2008): "The centred parametrization for the multivariate skew-normal distribution". Journal of Multivariate Analysis, Volume 99, Issue 7, 1362-1382.

## See Also

```
stdEr, vcov
```

# **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.

ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))

ChinaT_NE <- mle(ChinaT)

# Display model estimates

print(coef(ChinaT_NE))

## Not run:

# Estimate Skew-Normal distribution parameters by maximum likelihood

ChinaT_SNE <- mle(ChinaT, Model="SKNormal")

# Display model estimates

print(coef(ChinaT_SNE, ParType="Centr"))

print(coef(ChinaT_SNE, ParType="Direct"))

## End(Not run)</pre>
```

ConfMat

Confussion Matrices for classification results

# Description

'ConfMat' creates confussion matrices from two factor describing, respectively, original classes and predicted classification results

## Usage

```
ConfMat(origcl, predcl, otp=c("absandrel", "abs", "rel"), dec=3)
```

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## **Arguments**

origcl A factor describing the original classes.

predcl A factor describing the predicted classes.

otp A string describing the output to be displayed and returned. Alternatives are

"absandrel" for two confusion matrices, respectively with absolute and relative frequencies, "abs" for a confusion matrix with absolute frequencies, and "rel"

for a confusion matrix relative frequencies.

dec The number of decimal digits to display in matrices of relative frequencies.

#### Value

When argument 'otp' is set to "absandrel" (default), a list with two confusion matrices, respectively with absolute and relative frequencies. When argument 'otp' is set to "abs" a confusion matrix with absolute frequencies, and when argument 'otp' is set to "rel" a confusion matrix with relative frequencies.

#### Author(s)

A. Pedro Duarte Silva

#### See Also

```
lda, qda, snda, Roblda, Robqda, DACrossVal
```

# **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.

ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))

#Linear Discriminant Analysis

ChinaT.lda <- lda(ChinaT, ChinaTemp$GeoReg)
ldapred <- predict(ChinaT.lda, ChinaT)$class

# lda resubstitution confusion matrix

ConfMat(ChinaTemp$GeoReg, ldapred)

#Quadratic Discriminant Analysis

ChinaT.qda <- qda(ChinaT, ChinaTemp$GeoReg)
qdapred <- predict(ChinaT.qda, ChinaT)$class

# qda resubstitution confusion matrix

ConfMat(ChinaTemp$GeoReg, qdapred)</pre>
```

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ConfTests-class

Class "Configuration Tests"

# Description

ConfTests contains a list of the results of statistical likelihood-ratio tests that evaluate the goodness-of-fit of restricted models against more general ones. Currently, the models implemented are those based on the Normal and Skew-Normal distributions, with the four alternative variance-covariance matrix configurations.

## Slots

TestRes: List of test results; each element is an object of class LRTest, with the following components:

ChiSq: Value of the Chi-Square statistics corresponding to the performed test.

df: Degrees of freedom of the Chi-Square statistics.

**pvalue**: p-value of the Chi-Square statistics value, obtained from the Chi-Square distribution with df degrees of freedom.

H0logLik: Logarithm of the Likelihood function under the null hypothesis.

**H1logLik**: Logarithm of the Likelihood function under the alternative hypothesis.

RestModels: The restricted model (corresponding to the null hypothesis)

FullModels: The full model (corresponding to the alternative hypothesis)

## Methods

```
show signature(object = "ConfTests"): show S4 method for the ConfTests-class
```

## Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

## See Also

mle, IData, LRTest

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cor--methods

Methods for function cor in Package 'MAINT.Data'

## **Description**

S4 methods for function cor. These methods extract estimates of correlation matrices for the models fitted to Interval Data.

# Usage

```
## S4 method for signature 'IdtNDE'
cor(x)
## S4 method for signature 'IdtSNDE'
cor(x)
## S4 method for signature 'IdtNandSNDE'
cor(x)
## S4 method for signature 'IdtMxNDE'
cor(x)
## S4 method for signature 'IdtMxSNDE'
cor(x)
```

## **Arguments**

Х

An object representing a model fitted to interval data.

## Value

For the IdtNDE, IdtSNDE and IdtNandSNDE methods or IdtMxNDE, IdtMxSNDE methods with slot "Hmcdt" equal to TRUE: a matrix with the estimated correlations.

For the IdtMxNDE, and IdtMxSNDE methods with slot "Hmcdt" equal to FALSE: a three-dimensional array with a matrix with the estimated correlations for each group at each level of the third dimension.

## See Also

var

# **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.
ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))
ChinaT_NE <- mle(ChinaT)</pre>
```

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```
# Display correlation estimates
print(cor(ChinaT_NE))
```

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Cross Validation for Discriminant Analysis Classification Rules

# Description

'DACrossVal' evaluates the performance of a Discriminant Analysis training sample algorithm by k-fold Cross-Validation.

# Usage

```
DACrossVal(data, grouping, TrainAlg, EvalAlg=EvalClrule, Strfolds=TRUE, kfold=10, CVrep=20, prior="proportions", loo=FALSE, dec=3, ...)
```

# **Arguments**

data	Matrix, data frame or Interval Data object of observations.
grouping	Factor specifying the class for each observation.
TrainAlg	A function with the training algorithm. It should return an object that can be used as input to the argument of 'EValAlg'.
EvalAlg	A function with the evaluation algorithm. By default set to 'EvalClrule' which returns a list with components "err" (estimates of error rates by class) and "Nk" (number of out-sample observations by class). This default can be used for all 'TrainAlg' arguments that return an object with a predict method returning a list with a 'class' component (a factor) containing the classification results.
Strfolds	Boolean flag indicating if the folds should be stratified according to the original class proportions (default), or randomly generated from the whole training sample, ignoring class membership.
kfold	Number of training sample folds to be created in each replication.
CVrep	Number of replications to be performed.
prior	The prior probabilities of class membership. If unspecified, the class proportions for the training set are used. If present, the probabilities should be specified in the order of the factor levels.
loo	A boolean flag indicating if a leave-one-out strategy should be employed. When set to "TRUE" overrides the kfold and CVrep arguments.
dec	The number of decimal digits to display in confusion matrices of relative frequencies.
	Further arguments to be passed to 'TrainAlg' and 'EvalAlg'.

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#### Value

A three dimensional array with the number of tested observations, and estimated classification errors for each combination of fold and replication tried. The array dimensions are defined as follows:

The first dimension runs through the different fold-replication combinations.

The second dimension represents the classes.

The third dimension has two named levels representing respectively the number of observations tested ("Nk"), and the estimated classification errors ("Clerr").

## Author(s)

A. Pedro Duarte Silva

#### See Also

lda, qda, IData

## **Examples**

```
## Not run:
# Compare performance of linear and quadratic discriminant analysis with
# Covariance cases C1 and c4 on the ChinaT data set by 5-fold cross-validation
# replicated twice
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.
ChinaT <- IData(ChinaTemp[1:8])</pre>
# Classical (configuration 1) Linear Discriminant Analysis
CVldaC1 <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=lda,CovCase=1,kfold=5,CVrep=2)</pre>
summary(CVldaC1[,,"Clerr"])
# Linear Discriminant Analysis with covariance case 3
CVldaC4 <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=lda,CovCase=3,kfold=5,CVrep=2)</pre>
summary(CVldaC4[,,"Clerr"])
# Classical (configuration 1) Quadratic Discriminant Analysis
CVqdaC1 <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=qda,CovCase=1,kfold=5,CVrep=2)</pre>
summary(CVqdaC1[,,"Clerr"])
# Quadratic Discriminant Analysis with covariance case 3
CVqdaC4 <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=qda,CovCase=3,kfold=5,CVrep=2)</pre>
summary(CVqdaC4[,,"Clerr"])
```

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## End(Not run)

EMControl Constructor function for objects of class EMControl

# Description

This function will create a control object of class EMControl containing the control parameters for the EM algorithm used in estimation of Gaussian mixtures by function Idtmclust.

# Usage

EMControl(nrep=0, maxiter=1000, convtol=0.01, protol=1e-3, seed=NULL, pertubfct=1,
 k2max=1e6, MaxVarGRt=1e6)

# Arguments

nrep	Number of replications (different randomly generated starting points) of the EM algorithm.
maxiter	Maximum number of iterations in each replication of the EM algorithm.
convtol	Numeric tolerance for testing the convergence of the EM algorithm. Convergence is assumed when the log-likelihood changes less than convtol.
protol	Numeric tolerance for the mixture proportions. Proportions below protol, considered to be zero, are not allowed.
seed	Starting value for random generator.
pertubfct	Perturbation factor used to control the degree similarity between the alternative randomly generated starting points of the EM algorithm. Increasing (decreasing) the value of pertubfct increases (decreases) the expected difference between the starting points generated.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Solutions in which any component has correlation matrix with condition number above k2max, are considered to be spurious solutions and are eliminated from the EM search.
MaxVarGRt	Maximal allowed ratio of variances across components. Solutions in which any variable has a ratio between its maximal and minimal (across components) variances above MaxVarGRt, are considered to be spurious solutions and are eliminated from the EM search.

# Value

An EMControl object

# See Also

Idtmclust

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EMControl-class	EM algorithm control parameters for fitting Gaussian mixtures to interval data.
	terval data.

# **Description**

This class contains the control parameters for the EM algorithm used in estimation of Gaussian mixtures by function Idtmclust. .

# **Objects from the Class**

Objects can be created by calls of the form new("EMControl", ...) or by calling the constructor-function EMControl.

## **Slots**

nrep Number of replications (different randomly generated starting points) of the EM algorithm.

maxiter Maximum number of iterations in each replication of the EM algorithm.

convtol Numeric tolerance for testing the convergence of the EM algorithm. Convergence is assumed when the log-likelihood changes less than convtol.

protol Numeric tolerance for the mixture proportions. Proportions below protol, considered to be zero, are not allowed.

seed Starting value for random generator.

## See Also

**EMControl** 

# **Description**

"extmatrix" is a simple extension of the base matrix class, that that accepts NULL objects as members.

## **Extends**

Class matrix, directly.

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fasttle-methods

Methods for Function fasttle in Package 'MAINT.Data'

# **Description**

Performs maximum trimmed likelihood estimation by the fasttle algorithm

# Usage

```
fasttle(Sdt,
    CovCase=1:4,
    SelCrit=c("BIC","AIC"),
    alpha=control@alpha,
    nsamp = control@nsamp,
    seed=control@seed,
    trace=control@trace,
    use.correction=control@use.correction,
    ncsteps=control@ncsteps,
    getalpha=control@getalpha,
    rawMD2Dist=control@rawMD2Dist,
    MD2Dist=control@MD2Dist,
    eta=control@eta,
    multiCmpCor=control@multiCmpCor,
    getkdblstar=control@getkdblstar,
    outlin=control@outlin,
    trialmethod=control@trialmethod,
    m=control@m,
    reweighted = control@reweighted,
    k2max = control@k2max,
    otpType=control@otpType,
    control=RobEstControl(), ...)
```

## **Arguments**

	object represen	
Sdt		

CovCase Configuration of the variance-covariance matrix: a set of integers between 1 and

4.

SelCrit The model selection criterion.

alpha Numeric parameter controlling the size of the subsets over which the trimmed

likelihood is maximized; roughly alpha\*nrow(Sdt) observations are used for computing the trimmed likelihood. Note that when argument 'getalpha' is set to "TwoStep" the final value of 'alpha' is estimated by a two-step procedure and the value of argument 'alpha' is only used to specify the size of the samples used

in the first step. Allowed values are between 0.5 and 1.

nsamp Number of subsets used for initial estimates.

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seed Initial seed for random generator, like .Random.seed, see rrcov.control.

trace Logical (or integer) indicating if intermediate results should be printed; defaults

to FALSE.

use.correction whether to use finite sample correction factors; defaults to TRUE.

ncsteps The maximum number of concentration steps used each iteration of the fasttle

algorithm.

getalpha Argument specifying if the 'alpha' parameter (roughly the percentage of the

sample used for computing the trimmed likelihood) should be estimated from the data, or if the value of the argument 'alpha' should be used instead. When set to "TwoStep", 'alpha' is estimated by a two-step procedure with the value of argument 'alpha' specifying the size of the samples used in the first step.

Otherwise, the value of argument 'alpha' is used directly.

rawMD2Dist The assumed reference distribution of the raw MCD squared distances, which is

used to find to cutoffs defining the observations kept in one-step reweighted MCD estimates. Alternatives are 'ChiSq', 'HardRockeAsF' and 'HardRockeAdjF', respectivelly for the usual Chi-square, and the asymptotic and adjusted

scaled F distributions proposed by Hardin and Rocke (2005).

MD2Dist The assumed reference distributions used to find cutoffs defining the observa-

tions assumed as outliers. Alternatives are "ChiSq" and "CerioliBetaF" respectivelly for the usual Chi-square, or the Beta and F distributions proposed by

Cerioli (2010).

eta Nominal size for the null hypothesis that a given observation is not an outlier.

Defines the raw MCD Mahalanobis distances cutoff used to choose the observa-

tions kept in the reweightening step.

multiCmpCor Whether a multicomparison correction of the nominal size (eta) for the outliers

tests should be performed. Alternatives are: 'never' – ignoring the multicomparisons and testing all entities at 'eta' nominal level. 'always' – testing all n entitites at 1.-  $(1.-\text{'eta'}^{(1/n)})$ ; and 'iterstep' – use the iterated rule proposed by Cerioli (2010), *i.e.*, make an initial set of tests using the nominal size 1.-  $(1-\text{'eta'}^{(1/n)})$ , and if no outliers are detected stop. Otherwise, make a second step

testing for outliers at the 'eta' nominal level.

getkdblstar Argument specifying the size of the initial small (in order to minimize the prob-

ability of outliers) subsets. If set to the string "Twopplusone" (default) the initial sets have twice the number of interval-value variables plus one (i.e., they are the smaller samples that lead to a non-singular covariance estimate). Otherwise, an

integer with the size of the initial sets.

outlin The type of outliers to be considered. "MidPandLogR" if outliers may be present

in both MidPpoints and LogRanges, "MidP" if outliers are only present in MidP-

points, or "LogR" if outliers are only present in LogRanges.

trialmethod The method to find a trial subset used to initialize each replication of the fasttle

algorithm. The current options are "simple" (default) that simply selects 'kd-blstar' observations at random, and "Poolm" that divides the original sample into 'm' non-overlaping subsets, applies the 'simple trial' and the refinement

methods to each one of them, and merges the results into a trial subset.

Number of non-overlaping subsets used by the trial method when the argument

of 'trialmethod' is set to 'Poolm'.

m

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reweighted Should a (Re)weighted estimate of the covariance matrix be used in the computation of the trimmed likelihood or just a "raw" covariance estimate; default is (Re)weighting. k2max

Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numeri-

cally singular, leading to degenerate results.

otpType The amount of output returned by fasttle. Current options are "SetMD2andEst"

(default) which returns an 'IdtSngNDRE' object with the fasttle estimates, a vector with the final trimmed subset elements used to compute these estimates

and the corresponding robust squared Mahalanobis distances, and

"SetMD2EstandPrfSt" wich returns an 'IdtSngNDRE' object with the previous slots plust a list of some performance statistics concerning the algorithm execu-

tion.

control a list with estimation options - this includes those above provided in the function

> specification. See RobEstControl for the defaults. If control is supplied, the parameters from it will be used. If parameters are passed also in the invocation statement, they will override the corresponding elements of the control object.

Further arguments to be passed to internal functions of fasttle.

#### Value

An object of class IdtE with the fasttle estimates, the value of the comparison criterion used to select the covariance configurations, the robust squared Mahalanobis distances, and optionally (if argument 'otpType' is set to true) performance statistics concerning the algorithm execution.

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. Journal of the American Statistical Association 105 (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. Advances in Data Analysis and Classification, 1–38.

Hadi, A. S. and Luceno, A. (1997), Maximum trimmed likelihood estimators: a unified approach, examples, and algorithms. Computational Statistics and Data Analysis 25(3), 251–272.

Hardin, J. and Rocke, A. (2005), The Distribution of Robust Distances. Journal of Computational and Graphical Statistics 14, 910–927.

Todorov V. and Filzmoser P. (2009), An Object Oriented Framework for Robust Multivariate Analysis. Journal of Statistical Software 32(3), 1–47.

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#### See Also

```
fulltle, RobEstControl, getIdtOutl, IdtSngNDRE
```

## **Examples**

```
## Not run:
 # Create an Interval-Data object containing the intervals of temperatures by quarter
 # for 899 Chinese meteorological stations.
 ChinaT <- IData(ChinaTemp[1:8])</pre>
 # Estimate parameters by the fast trimmed maximum likelihood estimator,
 # using a two-step procedure to select the trimming parameter, a reweighted
 # MCD estimate, and the classical 97.5% chi-square quantile cut-offs.
 Chinafasttle1 <- fasttle(ChinaT)</pre>
 cat("China maximum trimmed likelihood estimation results =\n")
 print(Chinafasttle1)
 # Estimate parameters by the fast trimmed maximum likelihood estimator, using
 # the triming parameter that maximizes breakdown, and a reweighted MCD estimate
 # based on the 97.5% quantiles of Hardin and Rocke adjusted F distributions.
 Chinafasttle2 <- fasttle(ChinaT,alpha=0.5,getalpha=FALSE,rawMD2Dist="HardRockeAdjF")
 cat("China maximum trimmed likelihood estimation results =\n")
 print(Chinafasttle2)
 # Estimate parameters by the fast trimmed maximum likelihood estimator, using a two-step procedure
 # to select the triming parameter, a reweighed MCD estimate based on Hardin and Rocke adjusted
 # F distributions, and 95% quantiles, and the Cerioli Beta and F distributions together
 # with Cerioli iterated procedure to identify outliers in the first step.
 Chinafasttle3 <- fasttle(ChinaT,rawMD2Dist="HardRockeAdjF",eta=0.05,MD2Dist="CerioliBetaF",
 multiCmpCor="iterstep")
 cat("China maximum trimmed likelihood estimation results =\n")
 print(Chinafasttle3)
 ## End(Not run)
fulltle-methods
                          Methods for Function fulltle in Package 'MAINT.Data'
```

## **Description**

Performs maximum trimmed likelihood estimation by an exact algorithm (full enumeratiom of all k-trimmed subsets)

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#### Usage

## **Arguments**

Sdt An IData object representing interval-valued units.

CovCase Configuration of the variance-covariance matrix: a set of integers between 1 and

4.

SelCrit The model selection criterion.

alpha Numeric parameter controlling the size of the subsets over which the trimmed

likelihood is maximized; roughly alpha\*nrow(Sdt) observations are used for computing the trimmed likelihood. Note that when argument 'getalpha' is set to "TwoStep" the final value of 'alpha' is estimated by a two-step procedure and the value of argument 'alpha' is only used to specify the size of the samples used

in the first step. Allowed values are between 0.5 and 1.

use.correction whether to use finite sample correction factors; defaults to TRUE.

getalpha Argument specifying if the 'alpha' parameter (roughly the percentage of the

sample used for computing the trimmed likelihood) should be estimated from the data, or if the value of the argument 'alpha' should be used instead. When set to "TwoStep", 'alpha' is estimated by a two-step procedure with the value of argument 'alpha' specifying the size of the samples used in the first step.

Otherwise, the value of argument 'alpha' is used directly.

rawMD2Dist The assumed reference distribution of the raw MCD squared distances, which

is used to find to cutoffs defining the observations kept in one-step reweighted MCD estimates. Alternatives are 'ChiSq', 'HardRockeAsF' and 'HardRockeAdjF', respectivelly for the usual Chi-square, and the asymptotic and adjusted

scaled F distributions proposed by Hardin and Rocke (2005).

MD2Dist The assumed reference distributions used to find cutoffs defining the observa-

tions assumed as outliers. Alternatives are "ChiSq" and "CerioliBetaF" respectivelly for the usual Chi-square, and the Beta and F distributions proposed by

Cerioli (2010).

eta Nominal size of the null hypothesis that a given observation is not an outlier.

Defines the raw MCD Mahalanobis distances cutoff used to choose the observa-

tions kept in the reweightening step.

multiCmpCor Whether a multicomparison correction of the nominal size (eta) for the outliers

tests should be performed. Alternatives are: 'never' – ignoring the multicomparisons and testing all entities at the 'eta' nominal level. 'always' – testing all n entitites at 1.-  $(1.-\text{'eta'}^{(1/n)})$ ; and 'iterstep' – use the iterated rule proposed

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by Cerioli (2010), *i.e.*, make an initial set of tests using the nominal size 1.- (1-'eta'^(1/n)), and if no outliers are detected stop. Otherwise, make a second step testing for outliers at the 'eta' nominal level.

outlin The type of outliers to be consideres. "MidPandLogR" if outliers may be present

in both MidPpoints and LogRanges, "MidP" if outliers are only present in MidP-

points, or "LogR" if outliers are only present in LogRanges.

reweighted should a (Re)weighted estimate of the covariance matrix be used in the compu-

tation of the trimmed likelihood or just a "raw" covariance estimate; default is

(Re)weighting.

k2max Maximal allowed 12-norm condition number for correlation matrices. Correla-

tion matrices with condition number above k2max are considered to be numeri-

cally singular, leading to degenerate results.

force A boolean flag indicating whether, for moderate or large data sets the algorithm

should proceed anyway, regardless of an expected long excution time, due to exponential explosions in the number of different subsets that need to be avaluated

by fulltle.

... Further arguments to be passed to internal functions of 'fulltle'.

#### Value

An object of class IdtE with the fulltle estimates, the value of the comparison criterion used to select the covariance configurations and the robust squared Mahalanobis distances.

# References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. *Journal of the American Statistical Association* **105** (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Hadi, A. S. and Luceno, A. (1997), Maximum trimmed likelihood estimators: a unified approach, examples, and algorithms. *Computational Statistics and Data Analysis* **25**(3), 251–272.

Hardin, J. and Rocke, A. (2005), The Distribution of Robust Distances. *Journal of Computational and Graphical Statistics* **14**, 910–927.

#### See Also

fasttle, getIdtOutl

getIdtOutl 25

## **Examples**

```
## Not run:
# Create an Interval-Data object containing the intervals for characteristics
# of 27 cars models.
CarsIdt <- IData(Cars[1:8], VarNames=c("Price", "EngineCapacity", "TopSpeed", "Acceleration"))</pre>
# Estimate parameters by the full trimmed maximum likelihood estimator,
# using a two-step procedure to select the trimming parameter, a reweighed
# MCD estimate, and the classical 97.5% chi-square quantile cut-offs.
CarsTE1 <- fulltle(CarsIdt)</pre>
cat("Cars data -- normal maximum trimmed likelihood estimation results:\n")
print(CarsTE1)
# Estimate parameters by the full trimmed maximum likelihood estimator, using
# the triming parameter that maximizes breakdown, and a reweighed MCD estimate
# based on the 97.5% quantiles of Hardin and Rocke adjusted F distributions.
CarsTE2 <- fulltle(CarsIdt,alpha=0.5,getalpha=FALSE,rawMD2Dist="HardRockeAdjF")</pre>
cat("Cars data -- normal maximum trimmed likelihood estimation results:\n")
print(CarsTE2)
# Estimate parameters by the full trimmed maximum likelihood estimator, using
# a two-step procedure to select the trimming parameter, and a reweighed MCD estimate
# based on Hardin and Rocke adjusted F distributions, 95% quantiles, and
# the Cerioli Beta and F distributions together with his iterated procedure
# to identify outliers in the first step.
CarsTE3 <- fulltle(CarsIdt,rawMD2Dist="HardRockeAdjf",eta=0.05,MD2Dist="CerioliBetaF",</pre>
multiCmpCor="iterstep")
cat("Cars data -- normal maximum trimmed likelihood estimation results:\n")
print(CarsTE3)
## End(Not run)
```

getIdtOutl

Get Interval Data Outliers

## **Description**

Identifies outliers in a data set of Interval-valued variables

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#### Usage

```
getIdtOut1(Sdt, IdtE=NULL, muE=NULL, SigE=NULL,
  eta=0.025, Rewind=NULL, m=length(Rewind),
  RefDist=c("ChiSq","HardRockeAdjF","HardRockeAsF","CerioliBetaF"),
  multiCmpCor=c("never","always","iterstep"),
  outlin=c("MidPandLogR","MidP","LogR"))
```

#### **Arguments**

Sdt An IData object representing interval-valued entities. IdtE Ao object of class IdtSngNDRE or IdtSngNDE containing mean and covariance estimates. muE Vector with the mean estimates used to find Mahalanobis distances. When specified, it overrides the mean estimate supplied in "IdtE". Matrix with the covariance estimates used to find Mahalanobis distances. When SigE specified, it overrides the covariance estimate supplied in "IdtE". eta Nominal size of the null hypothesis that a given observation is not an outlier. Rewind A vector with the subset of entities used to compute trimmed mean and covariance estimates when using a reweighted MCD. Only used when the 'RefDist' argument is set to "CerioliBetaF." Number of entities used to compute trimmed mean and covariance estimates m when using a reweighted MCD. Not used when the 'RefDist' argument is set to "ChiSq." multiCmpCor Whether a multicomparison correction of the nominal size (eta) for the outliers tests should be performed. Alternatives are: 'never' - ignoring the multicomparisons and testing all entities at the 'eta' nominal level. 'always' – testing all n entitites at 1.- (1.-'eta'^(1/n)); and 'iterstep' – use the iterated rule proposed by Cerioli (2010), i.e., make an initial set of tests using the nominal size 1.- (1-'eta'^(1/n)), and if no outliers are detected stop. Otherwise, make a second step testing for outliers at the 'eta' nominal level. RefDist The assumed reference distributions used to find cutoffs defining the observations assumed as outliers. Alternatives are "ChiSq", "HardRockeAsF", "HardRockeAdjF" and "CerioliBetaF", respectivelly for the usual Chi-squared, the asymptotic and adjusted scaled F distributions proposed by Hardin and Rocke (2005), and the Beta and F distributions proposed by Cerioli (2010).

The type of outliers to be considered. "MidPandLogR" if outliers may be present

in both MidPpoints and LogRanges, "MidP" if outliers are only present in MidP-

points, or "LogR" if outliers are only present in LogRanges.

## Value

outlin

A vector with the indices of the entities identified as outliers.

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#### References

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. *Journal of the American Statistical Association* **105** (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Hardin, J. and Rocke, A. (2005), The Distribution of Robust Distances. *Journal of Computational and Graphical Statistics* **14**, 910–927.

## See Also

```
fasttle, fulltle
```

## **Examples**

```
## Not run:
# Create an Interval-Data object containing the intervals for characteristics
# of 27 cars models.
CarsIdt <- IData(Cars[1:8], VarNames=c("Price", "EngineCapacity", "TopSpeed", "Acceleration"))</pre>
# Estimate parameters by the fast trimmed maximum likelihood estimator,
# using a two-step procedure to select the trimming parameter, a reweighed
# MCD estimate, and the classical 97.5% chi-squared quantile cut-offs.
Carstle1 <- fulltle(CarsIdt)</pre>
# Get and display the outliers using the classical 97.5% chi-squared quantile cut-offs.
CarsOtl1 <- getIdtOutl(CarsIdt,Carstle1)</pre>
print(CarsOtl1)
plot(CarsOtl1)
# Estimate parameters by the fast trimmed maximum likelihood estimator,
# using a two-step procedure to select the trimming parameter, and a reweighed
# based on the 97.5% quantiles of Hardin and Rocke adjusted F distributions.
Carstle2 <- fulltle(CarsIdt,rawMD2Dist="HardRockeAdjF")</pre>
# Get and display the outliers using the 97.5
CarsTtl2 <- getIdtOutl(CarsIdt,Carstle2,RefDist="CerioliBetaF")</pre>
print(CarsTtl2)
plot(CarsTtl2)
## End(Not run)
```

28 IData

IData	Interval Data objects

## **Description**

IData creates IData objects from data frames of interval bounds or MidPoint/LogRange values of the interval-valued observations.

# Usage

```
IData(Data,
Seq = c("LbUb_VarbyVar", "MidPLogR_VarbyVar", "AllLb_AllUb", "AllMidP_AllLogR"),
VarNames=NULL, ObsNames=row.names(Data), NbMicroUnits=integer(0))
```

## **Arguments**

Data	a data frame or matrix of interval bounds or MidPoint/LogRange values.

Seq the format of 'Data' data frame. Available options are:

"LbUb\_VarbyVar": lower bounds followed by upper bounds, variable by vari-

abic.

"MidPLogR\_VarbyVar": MidPoints followed by LogRanges, variable by vari-

able.

"AllLb\_AllUb": all lower bounds followed by all upper bounds, in the same

variable order.

"AllMidP\_AllLogR": all MidPoints followed all LogRanges, in the same vari-

able order.

VarNames An optional vector of names to be assigned to the Interval-Valued Variables.

ObsNames An optional vector of names assigned to the individual observations.

NbMicroUnits An integer vector with the number of micro data units by interval-valued obser-

vation (or an empty vector, if not applicable)

## **Details**

Objects of class IData describe a data set of 'NObs' observations on 'NIVar' Interval-valued variables. This function creates an interval-data object from a data-frame with either the lower and upper bounds of the observed intervals or by their midpoints and log-ranges.

#### See Also

IData, AgrMcDt

IData-class 29

## **Examples**

```
ChinaT <- IData(ChinaTemp[1:8],VarNames=c("T1","T2","T3","T4"))
cat("Summary of the ChinaT IData object:\n") ; print(summary(ChinaT))
cat("ChinaT first ant last three observations:\n")
print(head(ChinaT,n=3))
cat("\n...\n")
print(tail(ChinaT,n=3))</pre>
```

IData-class

Class IData

## **Description**

A data-array of interval-valued data is an array where each of the NObs rows, corresponding to each entity under analysis, contains the observed intervals of the NIVar descriptive variables.

#### Slots

MidP: A data-frame of the midpoints of the observed intervals

LogR: A data-frame of the logarithms of the ranges of the observed intervals

ObsNames: An optional vector of names assigned to the individual observations.

VarNames: An optional vector of names to be assigned to the Interval-valued Variables.

NObs: Number of entities under analysis (cases)

NIVar: Number of interval variables

NbMicroUnits: An integer vector with the number of micro data units by interval-valued observation (or an empty vector, if not applicable)

# Methods

```
show signature(object = "IData"): show S4 method for the IData-class.
```

**nrow** signature(x = "IData"): returns the number of statistical units (observations).

**ncol** signature(x = "IData"): returns the number of of Interval-valued variables.

**dim** signature(x = "IData"): returns a vector with the of number statistical units as first element, and the number of Interval-valued variables as second element.

rownames signature(x = "IData"): returns the row (entity) names for an object of class IData.

colnames signature(x = "IData"): returns column (variable) names for an object of class IData.

names signature(x = "IData"): returns column (variable) names for an object of class IData.

**MidPoints** signature(Sdt = "IData"): returns a data frame with MidPoints for an object of class IData.

LogRanges signature(Sdt = "IData"): returns a data frame with LogRanges for an object of class IData.

**Ranges** signature(Sdt = "IData"): returns an data frame with Ranges for an object of class IData.

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**NbMicroUnits** signature(Sdt = "IData"): returns an integer vector with the number of micro data units by interval-valued observation for an object of class IData.

**head** signature(x = "IData"): head S4 method for the IData-class.

tail signature(x = "IData"): tail S4 method for the IData-class.

plot signature(x = "IData"): plot S4 methods for the IData-class.

**mle** signature(x = "IData"): Maximum likelihood estimation.

**fasttle** signature(x = "IData"): Fast trimmed maximum likelihood estimation.

**fulltle** signature(x = "IData"): Exact trimmed maximum likelihood estimation.

**RobMxtDEst** signature(x = "IData"): Robust estimation of distribution mixtures for intervalvalued data.

**MANOVA** signature(x = "IData"): MANOVA tests on the interval-valued data.

**Ida** signature(x = "IData"): Linear Discriminant Analysis using maximum likelihood parameter estimates of Gaussian mixtures.

**qda** signature(x = "IData"): Quadratic Discriminant Analysis using maximum likelihood parameter estimates of Gaussian mixtures.

**Roblda** signature(x = "IData"): Linear Discriminant Analysis using robust estimates of location and scatter.

**Robqda** signature(x = "IData"): Quadratic Discriminant Analysis using robust estimates of location and scatter.

snda signature(x = "IData"): Discriminant Analysis using maximum likelihood parameter estimates of SkewNormal mixtures.

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

# References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Noirhomme-Fraiture, M., Brito, P. (2011), Far Beyond the Classical Data Models: Symbolic Data Analysis. *Statistical Analysis and Data Mining* **4**(2), 157–170.

## See Also

IData, AgrMcDt, mle, fasttle, fulltle, RobMxtDEst, MANOVA, lda, qda, Roblda, Robqda

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IdtE-class

Class IdtE

#### **Description**

IdtE contains estimation results for the models assumed for single distributions, or mixtures of distributions, underlying data sets of interval-valued entities.

#### **Slots**

ModelNames: The model acronym, indicating the model type (currently, N for Normal and SN for Skew-Normal), and the configuration (Case 1 through Case 4)

ModelType: Indicates the model; currently, Gaussian or Skew-Normal distributions are implemented

ModelConfig: Configuration of the variance-covariance matrix: Case 1 through Case 4

NIVar: Number of interval variables

SelCrit: The model selection criterion; currently, AIC and BIC are implemented

logLiks: The logarithms of the likelihood function for the different cases

AICs: Value of the AIC criterion

BICs: Value of the BIC criterion

BestModel: Bestmodel indicates the best model according to the chosen selection criterion

SngD: Boolean flag indicating whether a single or a mixture of distribution were estimated

#### Methods

**BestModel** signature(Sdt = "IdtE"): Selects the best model according to the chosen selection criterion (currently, AIC or BIC)

show signature(object = "IdtE"): show S4 method for the IDtE-class

summary signature(object = "IdtE"): summary S4 method for the IDtE-class

**testMod** signature(Sdt = "IdtE"): Performs statistical likelihood-ratio tests that evaluate the goodness-of-fit of a nested model against a more general one.

sd signature(Sdt = "IdtE"): extracts the standard deviation estimates from objects of class IdtE.

**AIC** signature(Sdt = "IdtE"): extracts the value of the Akaike Information Criterion from objects of class IdtE.

**BIC** signature(Sdt = "IdtE"): extracts the value of the Bayesian Information Criterion from objects of class IdtE.

logLik signature(Sdt = "IdtE"): extracts the value of the maximised log-likelihood from objects of class IdtE.

mean signature(x = "IdtE"): extracts the mean vector estimate from objects of class IdtE

var signature(x = "IdtE"): extracts the variance-covariance matrix estimate from objects of class IdtE

cor signature(x = "IdtE"): extracts the correlation matrix estimate from objects of class IdtE

32 Idtlda-class

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

#### See Also

```
mle, fasttle, fulltle, MANOVA, RobMxtDEst, IData
```

Idtlda-class

Class "Idtlda"

## **Description**

Idtlda contains the results of Linear Discriminant Analysis for the interval data

## **Slots**

prior: Prior probabilities of class membership; if unspecified, the class proportions for the training set are used; if present, the probabilities should be specified in the order of the factor levels.

means: Matrix with the mean vectors for each group

scaling: Matrix which transforms observations to discriminant functions, normalized so that within groups covariance matrix is spherical.

N: Number of observations

CovCase: Configuration case of the variance-covariance matrix: Case 1 through Case 4

#### Methods

predict signature(object = "Idtlda"): Classifies interval-valued observations in conjunction
 with lda.

show signature(object = "Idtlda"): show S4 method for the IDdtlda-class

CovCase signature(object = "Idtlda"): Returns the configuration case of the variance-covariance
matrix

# Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt> IdtMANOVA-class 33

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

## See Also

qda, MANOVA, Roblda, Robqda, snda, IData

IdtMANOVA-class

Class IdtMANOVA

## **Description**

IdtMANOVA extends LRTest directly, containing the results of MANOVA tests on the intervalvalued data. This class is not used directly, but is the basis for different specializations according to the model assumed for the distribution in each group. In particular, the following specializations of IdtMANOVA are currently implemented:

IdtClMANOVA extends IdtMANOVA, assuming a classical (i.e., homoscedastic gaussian) setup.

IdtHetNMANOVA extends IdtMANOVA, assuming a heteroscedastic gaussian set-up.

IdtLocSNMANOVA extends IdtMANOVA, assuming a Skew-Normal location model set-up.

IdtLocNSNMANOVA extends IdtMANOVA, assuming either a homoscedastic gaussian or Skew-Normal location model set-up.

IdtGenSNMANOVA extends IdtMANOVA, assuming a Skew-Normal general model set-up.

IdtGenNSNMANOVA extends IdtMANOVA, assuming either a heteroscedastic gaussian or Skew-Normal general model set-up.

## **Slots**

NIVar: Number of interval variables.

grouping: Factor indicating the group to which each observation belongs to.

Hores: Model estimates under the null hypothesis.

H1res: Model estimates under the alternative hypothesis.

ChiSq: Inherited from class LRTest. Value of the Chi-Square statistics corresponding to the performed test.

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df: Inherited from class LRTest. Degrees of freedom of the Chi-Square statistics.

pvalue: Inherited from class LRTest. p-value of the Chi-Square statistics value, obtained from the Chi-Square distribution with df degrees of freedom.

H0logLik: Inherited from class LRTest. Logarithm of the Likelihood function under the null hypothesis.

H1logLik: Inherited from class LRTest. Logarithm of the Likelihood function under the alternative hypothesis.

## Methods

**show** signature(object = "IdtMANOVA"): show S4 method for the IdtMANOVA-classes.

**summary** signature(object = "IdtMANOVA"): summary S4 method for the IdtMANOVA-classes.

**H0res** signature(object = "IdtMANOVA"): retrieves the model estimates under the null hypothesis

**H1res** signature(object = "IdtMANOVA"): retrieves the model estimates under the alternative hypothesis.

**Ida** signature(x = "IdtClMANOVA"): Linear Discriminant Analysis using the estimated model parameters.

**lda** signature(x = "IdtLocNSNMANOVA"): Linear Discriminant Analysis using the estimated model parameters.

**qda** signature(x = "IdtHetNMANOVA"): Quadratic Discriminant Analysis using the estimated model parameters.

**qda** signature(x = "IdtGenNSNMANOVA"): Quadratic Discriminant Analysis using the estimated model parameters.

snda signature(x = "IdtLocNSNMANOVA"): Discriminant Analysis using maximum likelihood parameter estimates of SkewNormal mixtures assuming a "location" model (i.e., groups differ only in location parameters).

**snda** signature(x = "IdtGenSNMANOVA"): Discriminant Analysis using maximum likelihood parameter estimates of SkewNormal mixtures assuming a general model (i.e., groups differ in all parameters).

snda signature(x = "IdtGenNSNMANOVA"): Discriminant Analysis using maximum likelihood parameter estimates of SkewNormal mixtures assuming a general model (i.e., groups differ in all parameters).

#### **Extends**

Class LRTest, directly.

## Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

# References

Brito, P., Duarte Silva, A. P. (2012): "Modelling Interval Data with Normal and Skew-Normal Distributions". Journal of Applied Statistics, Volume 39, Issue 1, 3-20.

IdtMclust-class 35

#### See Also

MANOVA, 1da, qda, snda, IData

IdtMclust-class

Class IdtMclust

# Description

IdtMclust contains the results of fitting mixtures of Gaussian distributions to interval data represented by objects of class IData.

#### Slots

call: The matched call that created the IdtMclust object

data: The IData data object

NObs: Number of entities under analysis (cases)

NIVar: Number of interval variables

SelCrit: The model selection criterion; currently, AIC and BIC are implemented

Hmcdt: Indicates whether the optimal model corresponds to a homoscedastic (TRUE) or a hetereocedasic (FALSE) setup

BestG: The optimal number of mixture components.

BestC: The configuration case of the variance-covariance matrix in the optimal model

logLiks: The logarithms of the likelihood function for the different models tried

logLik: The logarithm of the likelihood function for the optimal model

AICs: The values of the AIC criterion for the different models tried

aic: The value of the AIC criterion for the he optimal model

BICs: The values of the BIC criterion for the different models tried

bic: The value of the BIC criterion for the he optimal model

parameters A list with the following components:

**pro** A vector whose *k*th component is the mixing proportion for the *k*th component of the mixture model.

**mean** The mean for each component. If there is more than one component, this is a matrix whose kth column is the mean of the kth component of the mixture model.

covariance A three-dimensional array with the covariance estimates. If Hmcdt is FALSE (heteroscedastic setups) the third dimension levels run through the BestG mixture components, with one different covariance matrix for each level. Otherwise (homoscedastic setups), there is only one covariance matrix and the size of the third dimension equals one.

z: A matrix whose [i,k]th entry is the probability that observation i in the test data belongs to the kth class.

classification: The classification corresponding to z, i.e. map(z).

allres: A list with the detailed results for all models fitted.

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#### Methods

show signature(object = "IdtMclust"): show S4 method for the IdtMclust-class

summary signature(object = "IdtMclust"): summary S4 method for the IdtMclust-class

parameters signature(x = "IdtMclust"): retrieves the value of the parameter estimates for the
 obtained partition

pro signature(x = "IdtMclust"): retrieves the value of the estimated mixing proportions for the
 obtained partition

mean signature(x = "IdtMclust"): retrieves the value of the component means for the obtained partition

var signature(x = "IdtMclust"): retrieves the value of the estimated covariance matrices for the obtained partition

**cor** signature(x = "IdtMclust"): retrieves the value of the estimated correlation matrices

classification signature(x = "IdtMclust"): retrieves the individual class assignments for the
 obtained partition

**SelCrit** signature(x = "IdtMclust"): retrieves a string specifying the criterion used to find the best model and partition

**Hmcdt** signature(x = "IdtMclust"): returns TRUE if an homecedastic model has been assumed, and FALSE otherwise

**BestG** signature(x = "IdtMclust"): returns the number of components selectd

**BestC** signature(x = "IdtMclust"): retruns the covariance configuration selected

**PostProb** signature(x = "IdtMclust"): retrieves the estimates of the individual posterir probabilities for the obtained partition

**BIC** signature(x = "IdtMclust"): returns the value of the BIC criterion

**AIC** signature(x = "IdtMclust"): returns the value of the AIC criterion

logLik signature(x = "IdtMclust"): returns the value of the log-likelihood

## Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

# References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Brito, P., Duarte Silva, A. P. and Dias, J. G. (2015), Probabilistic Clustering of Interval Data. *Intelligent Data Analysis* **19**(2), 293–313.

#### See Also

Idtmclust, plotInfCrt, pcoordplot

Idtmclust-methods 37

Idtmclust-methods	Methods for function Idtmclust in Package 'MAINT.Data'	

# **Description**

Performs Gaussian model based clustering for interval data

# Usage

```
Idtmclust(Sdt, G = 1:9, CovCase=1:4, SelCrit=c("BIC","AIC"),
    Mxt=c("Hom","Het","HomandHet"), control=EMControl())
```

### **Arguments**

Sdt	An IData object representing interval-valued entities.
G	An integer vector specifying the numbers of mixture components (clusters) for which the BIC is to be calculated.
CovCase	Configuration of the variance-covariance matrix: a set of integers between 1 and 4.
SelCrit	The model selection criterion.
control	A list of control parameters for EM. The defaults are set by the call ${\sf EMControl}$ ().
Mxt	The type of Gaussian mixture assumed by Idtmclust. Alternatives are "Hom" (default) for homoscedastic mixtures, "Het" for heteroscedastic mixtures, and "HomandHet" for both homoscedastic and heteroscedastic mixtures.

#### Value

An object of class IdtMclust providing the optimal (according to BIC) mixture model estimation.

### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Brito, P., Duarte Silva, A. P. and Dias, J. G. (2015), Probabilistic Clustering of Interval Data. *Intelligent Data Analysis* **19**(2), 293–313.

Fraley, C., Raftery, A. E., Murphy, T. B. and Scrucca, L. (2012), mclust Version 4 for R: Normal Mixture Modeling for Model-Based Clustering, Classification, and Density Estimation. Technical Report No. 597, Department of Statistics, University of Washington.

### See Also

IdtMclust, EMControl, EMControl, plotInfCrt, pcoordplot

38 IdtMxE-class

### **Examples**

```
## Not run:
# Create an Interval-Data object containing the intervals of loan data
# (from the Kaggle Data Science platform) aggregated by loan purpose
LbyPIdt <- IData(LoansbyPurpose_minmaxDt,</pre>
                 VarNames=c("ln-inc","ln-revolbal","open-acc","total-acc"))
print(LbyPIdt)
#Fit homoscedastic Gaussian mixtures with up to nine components
mclustres <- Idtmclust(LbyPIdt)</pre>
plotInfCrt(mclustres,legpos="bottomright")
print(mclustres)
#Display the results of the best mixture according to the BIC
summary(mclustres,parameters=TRUE,classification=TRUE)
pcoordplot(mclustres)
#Repeat the analysus with both homoscedastic and heteroscedastic mixtures up to six components
mclustres1 <- Idtmclust(LbyPIdt,G=1:6,Mxt="HomandHet")</pre>
plotInfCrt(mclustres1,legpos="bottomright")
print(mclustres1)
#Display the results of the best heteroscedastic mixture according to the BIC
summary(mclustres1,parameters=TRUE,classification=TRUE,model="HetG2C2")
## End(Not run)
```

IdtMxE-class

Class IdtMxE

# Description

IdtMxE extends the IdtE class, assuming that the data can be characterized by a mixture of distributions, for instances considering partitions of entities into different groups.

#### **Slots**

```
grouping: Factor indicating the group to which each observation belongs to

ModelNames: Inherited from class IdtE. The model acronym, indicating the model type (currently,
N for Normal and SN for Skew-Normal), and the configuration (Case 1 through Case 4)
```

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ModelType: Inherited from class IdtE. Indicates the model; currently, Gaussian or Skew-Normal distributions are implemented.

ModelConfig: Inherited from class IdtE. Configuration of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Bestmodel indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to FALSE in objects of class "IdtMxE"

Ngrps: Number of mixture components

### **Extends**

Class IdtE, directly.

#### Methods

No methods defined with class "IdtMxE" in the signature.

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt>
Paula Brito <mpbrito.fep.up.pt>

### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

### See Also

IdtE, IdtSngDE, IData, MANOVA, RobMxtDEst

40 IdtMxNandSNDE-class

IdtMxNandSNDE-class Class IdtMxNandSNDE

### **Description**

IdtMxNandSNDE contains the results of a mixture model estimation; Normal an Skew-Normal models are considered, with the four different possible variance-covariance configurations.

#### Slots

NMod: Estimates of the mixture model for the Gaussian case

SNMod: Estimates of the mixture model for the Skew-Normal case

grouping: Inherited from class IdtMxE. Factor indicating the group to which each observation belongs to

ModelNames: Inherited from class IdtE. The model acronym, indicating the model type (currently, N for Normal and SN for Skew-Normal), and the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; currently, Gaussian or Skew-Normal distributions are implemented

ModelConfig: Inherited from class IdtE. Configuration case of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to FALSE in objects of class IdtMxNandSNDE

Ngrps: Inherited from class IdtMxE. Number of mixture components

#### **Extends**

Class IdtMxE, directly. Class IdtE, by class IdtMxE, distance 2.

#### Methods

No methods defined with class IdtMxNandSNDE in the signature.

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt> IdtMxNDE-class 41

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

#### See Also

IdtE, IdtMxE, IdtSngNandSNDE, MANOVA, RobMxtDEst, IData

IdtMxNDE-class

Class IdtMxNDE

### **Description**

IdtMxNDE contains the results of a mixture Normal model maximum likelihood parameter estimation, with the four different possible variance-covariance configurations.

#### Slots

Hmcdt: Indicates whether we consider an homocedastic (TRUE) or a hetereocedasic model (FALSE)

mleNmuE: Matrix with the maximum likelihood mean vectors estimates by group (each row refers to a group)

mleNmuEse: Matrix with the maximum likelihood means' standard errors by group (each row refers to a group)

CovConfCases: List of the considered configurations

grouping: Inherited from class IdtMxE. Factor indicating the group to which each observation belongs to

ModelNames: Inherited from class IdtE. The model acronym formed by a "N", indicating a Normal model, followed by the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; always set to "Normal" in objects of the IdtMxNDE class

ModelConfig: Inherited from class IdtE. Configuration case of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to FALSE in objects of class IdtMxNDE

Ngrps: Inherited from class IdtMxE. Number of mixture components

42 IdtMxNDRE-class

#### **Extends**

Class IdtMxE, directly. Class IdtE, by class IdtMxE, distance 2.

#### Methods

**lda** signature(x = "IdtMxtNDE"): Linear Discriminant Analysis using the estimated model parameters.

**qda** signature(x = "IdtMxtNDE"): Quadratic Discriminant Analysis using the estimated model parameters.

# Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

#### See Also

IdtE, IdtMxE, IdtMxNDRE, IdtSngNDE, IData, MANOVA

IdtMxNDRE-class

Class IdtMxNDE

# **Description**

IdtMxNDRE contains the results of a mixture Normal model robust parameter estimation, with the four different possible variance-covariance configurations.

#### Slots

Hmcdt: Indicates whether we consider an homocedastic (TRUE) or a hetereocedasic model (FALSE)

RobNmuE: Matrix with the robust mean vectors estimates by group (each row refers to a group)

CovConfCases: List of the considered configurations

grouping: Inherited from class IdtMxE. Factor indicating the group to which each observation belongs to

ModelNames: Inherited from class IdtE. The model acronym formed by a "N", indicating a Normal model, followed by the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; always set to "Normal" in objects of the IdtMxNDRE class

ModelConfig: Inherited from class IdtE. Configuration case of the variance-covariance matrix: Case 1 through Case 4

IdtMxNDRE-class 43

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to FALSE in objects of class IdtMxNDRE

Ngrps: Inherited from class IdtMxE. Number of mixture components

rawSet A vector with the trimmed subset elements used to compute the raw (not reweighted) MCD covariance estimate for the chosen configuration.

RewghtdSet A vector with the final trimmed subset elements used to compute the fasttle estimates.

RobMD2 A vector with the robust squared Mahalanobis distances used to select the trimmed subset.

cnp2 A vector of length two containing the consistency correction factor and the finite sample correction factor of the final estimate of the covariance matrix.

raw.cov A matrix with the raw MCD estimator used to compute the robust squared Mahalanobis distances of RobMD2.

raw.cnp2 A vector of length two containing the consistency correction factor and the finite sample correction factor of the raw estimate of the covariance matrix.

PerfSt A a list with the following components:

**RepSteps**: A list with one component by Covariance Configuration, containing a vector with the number of refinement steps performed by the fasttle algorithm by replication.

**RepLogLik**: A list with one component by Covariance Configuration, containing a vector with the best log-likelihood found be fasttle algorithm by replication.

**StpLogLik**: A list with one component by Covariance Configuration, containing a matrix with the evolution of the log-likelihoods found be fasttle algorithm by replication and refinement step.

#### **Extends**

Class IdtMxE, directly. Class IdtE, by class IdtMxE, distance 2.

#### Methods

No methods defined with class IdtMxNDRE in the signature.

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt>
Paula Brito <mpbrito.fep.up.pt>

44 IdtMxSNDE-class

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

#### See Also

IdtE, IdtMxE, IdtMxNDE, IdtSngNDRE, RobMxtDEst, IData

IdtMxSNDE-class

Class IdtMxSNDE

### **Description**

IdtMxSNDE contains the results of a mixture model estimation for the Skew-Normal model, with the four different possible variance-covariance configurations.

#### **Slots**

Hmcdt: Indicates whether we consider an homoscedastic location model (TRUE) or a general model (FALSE)

CovConfCases: List of the considered configurations

grouping: Inherited from class IdtMxE. Factor indicating the group to which each observation belongs to

ModelNames: Inherited from class IdtE. The model acronym, indicating the model type (currently, N for Normal and SN for Skew-Normal), and the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; currently, Gaussian or Skew-Normal distributions are implemented

ModelConfig: Inherited from class IdtE. Configuration case of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to FALSE in objects of class IdtMxSNDE

Ngrps: Inherited from class IdtMxE. Number of mixture components

IdtMxtNDE-class 45

### **Extends**

Class IdtMxE, directly. Class IdtE, by class IdtMxE, distance 2.

#### Methods

No methods defined with class IdtMxSNDE in the signature.

## Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

### See Also

IdtE, IdtMxE, IdtSngSNDE, MANOVA, IData

IdtMxtNDE-class

Class IdtMxtNDE

### **Description**

IdtMxtNDE is an union of classes IdtMxNDE and IdtMxNDRE, containing the results of mixture Normal model parameter estimation by maximum likelihood (IdtMxNDE) or robust (IdtMxNDRE) methods.

### See Also

IdtE, IdtMxE, IdtMxNDE, IdtMxNDRE

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IdtNandSNDE-class

Class IdtNandSNDE

### **Description**

IdtNandSNDE is a union of classes IdtSngNandSNDE and IdtMxNandSNDE, used for storing the estimation results of Normal and Skew-Normal modelisations for Interval Data.

#### Methods

- coef signature(coef = "IdtNandSNDE"): extracts parameter estimates from objects of class Idt-NandSNDE
- stdEr signature(x = "IdtNandSNDE"): extracts standard errors from objects of class IdtNand-SNDE
- **vcov** signature(x = "IdtNandSNDE"): extracts an estimate of the variance-covariance matrix of the parameters estimators for objects of class IdtNandSNDE
- var signature(x = "IdtNandSNDE"): extracts the variance-covariance matrix estimate from objects of class IdtNandSNDE
- cor signature(x = "IdtNandSNDE"): extracts the correlation matrix estimate from objects of class IdtNandSNDE

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

### See Also

IData, mle, fasttle, fulltle, MANOVA, RobMxtDEst, IdtSngNandSNDE, IdtMxNandSNDE

IdtNDE-class

Class IdtNDE

### **Description**

IdtNDE is a a union of classes IdtSngNDE, IdtSngNDRE, IdtMxNDE and IdtMxNDRE, used for storing the estimation results of Normal modelizations for Interval Data.

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#### Methods

coef signature(coef = "IdtNDE"): extracts parameter estimates from objects of class IdtNDE

stdEr signature(x = "IdtNDE"): extracts standard errors from objects of class IdtNDE

**vcov** signature(x = "IdtNDE"): extracts an estimate of the variance-covariance matrix of the parameters estimators for objects of class IdtNDE

mean signature(x = "IdtNDE"): extracts the mean vector estimate from objects of class IdtNDE

var signature(x = "IdtNDE"): extracts the variance-covariance matrix estimate from objects of class IdtNDE

cor signature(x = "IdtNDE"): extracts the correlation matrix estimate from objects of class Idt-NDE

sd signature(Idt = "IdtNDE"): extracts the standard deviation estimates from objects of class IdtNDE.

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

#### See Also

IdtSngNDE, IdtSngNDRE, IdtMxNDE, IdtMxNDRE, IdtSNDE, IData, mle, fasttle, fulltle, MANOVA,
RobMxtDEst

IdtOutl-class

Class IdtOutl

### **Description**

A description of interval-valued variable outliers found by the MAINT.Data function getIdtOut1.

#### Slots

outliers: A vector of indices of the interval data units flaged as outliers.

MD2: A vector of squared robust Mahalanobis distances for all interval data units.

eta Nominal size of the null hypothesis that a given observation is not an outlier.

**RefDist** The assumed reference distributions used to find cutoffs defining the observations assumed as outliers. Alternatives are "ChiSq" and "CerioliBetaF" respectively for the usual Chi-squared, and the Beta and F distributions proposed by Cerioli (2010).

**multiCmpCor** Whether a multicomparison correction of the nominal size (eta) for the outliers tests was performed. Alternatives are: 'never' – ignoring the multicomparisons and testing all entities at the 'eta' nominal level. 'always' – testing all n entities at 1.- (1.- 'eta'^(1/n)).

**NObs** Number of original observations in the original data set.

p Number of total numerical variables (MidPoints and/or LogRanges) that may be responsible for the outliers. 48 IdtOutl-methods

h Size of the subsets over which the trimmed likelihood was maximized when computing the robust Mahalanobis distances.)

**boolRewind** A logical vector indicanting which of the data units belong to the final trimmed subsetused to compute the tle estimates.)

#### Methods

**show** signature(object = "IdtOutl"): show S4 method for the IdtOutl-class.

**plot** signature(x = "IdtOut1"): plot S4 methods for the IdtOutl-class.

**getMahaD2** signature(x = "IdtOut1"): retrieves the vector of squared robust Mahalanobis distances for all data units.

**geteta** signature(x = "IdtOutl"): retrieves the nominal size of the null hypothesis used to flag observations as outliers.

**getRefDist** signature(x = "IdtOutl"): retrieves the assumed reference distributions used to find cutoffs defining the observations assumed as outliers.

**getmultiCmpCor** signature(x = "IdtOut1"): retrieves the multicomparison correction used when flaging observations as outliers.

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. *Journal of the American Statistical Association* **105** (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

### See Also

```
getIdtOutl, fasttle, fulltle
```

IdtOutl-methods

Plot method for class IdtOutl in Package 'MAINT.Data'

# Description

Plots robust Mahalanobis distances and outlier cut-offs for an object describing potential outliers in a interval-valued data set

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### Usage

```
## S4 method for signature 'IdtOutl,missing'
plot(x, scale=c("linear","log"), RefDist=getRefDist(x), eta=geteta(x),
    multiCmpCor=getmultiCmpCor(x), ...)
```

### **Arguments**

x An IData object of class IdtOutl describing potential interval-valued ouliters.

scale The scale of the axis for the robust Mahalanobis distances.

RefDist The assumed reference distributions used to find cutoffs defining the observa-

tions assumed as outliers. Alternatives are "ChiSq" and "CerioliBetaF" respectively for the usual Chi-squared, and the Beta and F distributions proposed by Cerioli (2010). By default uses the one selected in the creation of the object 'x'.

eta Nominal size of the null hypothesis that a given observation is not an outlier. By

default uses the one selected in the creation of the object 'x'.

multiCmpCor Whether a multicomparison correction of the nominal size (eta) for the outliers

tests was performed. Alternatives are: 'never' – ignoring the multicomparisons and testing all entities at the 'eta' nominal level. 'always' – testing all n entitites at 1.-  $(1.-\text{'eta'}^{(1/n)})$ . By default uses the one selected in the creation of the

object 'x'.

. . . Further arguments to be passed to methods.

#### References

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. *Journal of the American Statistical Association* **105** (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Journal of Computational and Graphical Statistics 14, 910–927.

### See Also

```
getIdtOutl, fasttle, fulltle
```

Idtqda-class	Class "Idtqda"
--------------	----------------

### Description

Idtqda contains the results of Quadratic Discriminant Analysis for the interval data

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#### Slots

prior: Prior probabilities of class membership; if unspecified, the class proportions for the training set are used; if present, the probabilities should be specified in the order of the factor levels.

means: Matrix with the mean vectors for each group

scaling: A three-dimensional array. For each group, g, scaling["g] is a matrix which transforms interval-valued observations so that within-groups covariance matrix is spherical.

ldet: Vector of half log determinants of the dispersion matrix.

lev: Levels of the grouping factor

CovCase: Configuration case of the variance-covariance matrix: Case 1 through Case 4

#### Methods

predict signature(object = "Idtqda"): Classifies interval-valued observations in conjunction
 with qda.

**show** signature(object = "Idtqda"): show S4 method for the Idtqda-class

**CovCase** signature(object = "Idtqda"): Returns the configuration case of the variance-covariance matrix

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

### See Also

qda, MANOVA, Robqda, IData

IdtSNDE-class

Class "IdtSNDE"

### **Description**

IdtSNDE is a class union of classes IdtSngSNDE and IdtMxSNDE, used for storing the estimation results of Skew-Normal modelizations for Interval Data.

IdtSNgenda-class 51

#### Methods

coef signature(coef = "IdtSNDE"): extracts parameter estimates from objects of class IdtSNDE

stdEr signature(x = "IdtSNDE"): extracts standard errors from objects of class IdtSNDE

**vcov** signature(x = "IdtSNDE"): extracts an asymptotic estimate of the variance-covariance matrix of the parameters estimators for objects of class IdtSNDE

mean signature(x = "IdtSNDE"): extracts the mean vector estimate from objects of class Idt-SNDE

var signature(x = "IdtSNDE"): extracts the variance-covariance matrix estimate from objects of class IdtSNDE

#### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

#### See Also

IData, mle, MANOVA, IdtSngSNDE, IdtMxSNDE, IdtNDE

IdtSNgenda-class

Class "IdtSNgenda"

### **Description**

IdtSNgenda contains the results of discriminant analysis for the interval data, based on a general Skew-Normal model.

#### **Slots**

prior: Prior probabilities of class membership; if unspecified, the class proportions for the training set are used; if present, the probabilities should be specified in the order of the factor levels.

ksi: Matrix with the direct location parameter ("ksi") estimates for each group.

eta: Matrix with the direct scaled sekwness parameter ("eta") estimates for each group.

scaling: For each group g, scaling[,,g] is a matrix which transforms interval-valued observations so that in each group the scale-association matrix ("Omega") is spherical.

mu: Matrix with the centred location parameter ("mu") estimates for each group.

gamma1: Matrix with the centred sekwness parameter ("gamma1") estimates for each group.

ldet: Vector of half log determinants of the dispersion matrix.

lev: Levels of the grouping factor.

CovCase: Configuration case of the variance-covariance matrix: Case 1 through Case 4

#### Methods

predict signature(object = "IdtSNgenda"): Classifies interval-valued observations in conjunction with snda.

show signature(object = "IdtSNgenda"): show S4 method for the IdtSNgenda-class

CovCase signature(object = "IdtSNgenda"): Returns the configuration case of the variancecovariance matrix

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt>
Paula Brito <mpbrito.fep.up.pt>

#### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

#### See Also

MANOVA, snda, IData

## Description

IdtSngNandSNDE contains the results of a single class model estimation for the Normal and the Skew-Normal distributions, with the four different possible variance-covariance configurations.

### **Slots**

NMod: Estimates of the single class model for the Gaussian case

SNMod: Estimates of the single class model for the Skew-Normal case

ModelNames: Inherited from class IdtE. The model acronym, indicating the model type (currently, N for Normal and SN for Skew-Normal), and the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; currently, Gaussian or Skew-Normal distributions are implemented

ModelConfig: Inherited from class IdtE. Configuration of the variance-covariance matrix: Case 1 through Case 4

IdtSngNDE-class 53

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Bestmodel indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to TRUE in objects of class IdtSngNandSNDE

#### **Extends**

Class IdtSngDE, directly. Class IdtE, by class IdtSngDE, distance 2.

#### Methods

No methods defined with class IdtSngNandSNDE in the signature.

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

# See Also

IData, IdtMxNandSNDE, mle, fasttle, fulltle

IdtSngNDE-class

Class IdtSngNDE

# Description

Contains the results of a single class maximum likelihood estimation for the Normal distribution, with the four different possible variance-covariance configurations.

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#### **Slots**

mleNmuE: Vector with the maximum likelihood mean vectors estimates

mleNmuEse: Vector with the maximum likelihood means' standard errors

CovConfCases: List of the considered configurations

ModelNames: Inherited from class IdtE. The model acronym formed by a "N", indicating a Normal model, followed by the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; always set to "Normal" in objects of the IdtSngNDE class

ModelConfig: Inherited from class IdtE. Configuration of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Bestmodel indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to TRUE in objects of class IdtSngNDE

#### **Extends**

Class IdtSngDE, directly. Class IdtE, by class IdtSngDE, distance 2.

#### Methods

No methods defined with class IdtSngNDE in the signature.

#### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

### See Also

IData, mle, IdtSngNDRE, IdtSngSNDE, IdtMxNDE

IdtSngNDRE-class 55

IdtSngNDRE-class Class IdtSngNDRE

#### **Description**

Contains the results of a single class robust estimation for the Normal distribution, with the four different possible variance-covariance configurations.

#### Slots

RobNmuE: Matrix with the maximum likelihood mean vectors estimates

CovConfCases: List of the considered configurations

ModelNames: Inherited from class IdtE. The model acronym formed by a "N", indicating a Normal model, followed by the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; always set to "Normal" in objects of the IdtSngNDRE class

ModelConfig: Inherited from class IdtE. Configuration of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Bestmodel indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to TRUE in objects of class IdtSngNDRE

rawSet A vector with the trimmed subset elements used to compute the raw (not reweighted) MCD covariance estimate for the chosen configuration.

RewghtdSet A vector with the final trimmed subset elements used to compute the tle estimates.

RobMD2 A vector with the robust squared Mahalanobis distances used to select the trimmed subset.

cnp2 A vector of length two containing the consistency correction factor and the finite sample correction factor of the final estimate of the covariance matrix.

raw.cov A matrix with the raw MCD estimator used to compute the robust squared Mahalanobis distances of RobMD2.

raw.cnp2 A vector of length two containing the consistency correction factor and the finite sample correction factor of the raw estimate of the covariance matrix.

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PerfSt A a list with the following components:

**RepSteps**: A list with one component by Covariance Configuration, containing a vector with the number of refinement steps performed by the fasttle algorithm by replication.

**RepLogLik**: A list with one component by Covariance Configuration, containing a vector with the best log-likelihood found be fasttle algorithm by replication.

**StpLogLik**: A list with one component by Covariance Configuration, containing a matrix with the evolution of the log-likelihoods found be fasttle algorithm by replication and refinement step.

### **Extends**

Class IdtSngDE, directly. Class IdtE, by class IdtSngDE, distance 2.

#### Methods

No methods defined with class IdtSngNDRE in the signature.

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

### See Also

IData, fasttle, fulltle, IdtSngNDE, IdtMxNDRE

 ${\tt IdtSngSNDE-class}$ 

Class IdtSngSNDE

### **Description**

Contains the results of a single class maximum likelihood estimation for the Skew-Normal distribution, with the four different possible variance-covariance configurations.

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#### Slots

CovConfCases: List of the considered configurations

ModelNames: The model acronym, indicating the model type (currently, N for Normal and SN for Skew-Normal), and the configuration Case (C1 to C4) for the covariance matrix

ModelNames: Inherited from class IdtE. The model acronym formed by a "SN", indicating a skew-Normal model, followed by the configuration (Case 1 through Case 4)

ModelType: Inherited from class IdtE. Indicates the model; always set to "SkewNormal" in objects of the IdtSngSNDE class

ModelConfig: Inherited from class IdtE. Configuration case of the variance-covariance matrix: Case 1 through Case 4

NIVar: Inherited from class IdtE. Number of interval variables

SelCrit: Inherited from class IdtE. The model selection criterion; currently, AIC and BIC are implemented

logLiks: Inherited from class IdtE. The logarithms of the likelihood function for the different cases

AICs: Inherited from class IdtE. Value of the AIC criterion

BICs: Inherited from class IdtE. Value of the BIC criterion

BestModel: Inherited from class IdtE. Indicates the best model according to the chosen selection criterion

SngD: Inherited from class IdtE. Boolean flag indicating whether a single or a mixture of distribution were estimated. Always set to TRUE in objects of class IdtSngSNDE

# **Extends**

Class IdtSngDE, directly. Class IdtE, by class IdtSngDE, distance 2.

#### Methods

No methods defined with class IdtSngSNDE in the signature.

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

### See Also

```
mle, IData, IdtSngNDE, IdtMxSNDE
```

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IdtSNlocda-class

Class "IdtSNlocda"

# Description

IdtSNlocda contains the results of Discriminant Analysis for the interval data, based on a location Skew-Normal model.

#### **Slots**

prior: Prior probabilities of class membership; if unspecified, the class proportions for the training set are used; if present, the probabilities should be specified in the order of the factor levels.

ksi: Matrix with the direct location parameter ("ksi") estimates for each group.

eta: Vector with the direct scaled skewness parameter ("eta") estimates.

scaling: Matrix which transforms observations to discriminant functions, normalized so that the within groups scale-association matrix ("Omega") is spherical.

mu: Matrix with the centred location parameter ("mu") estimates for each group.

gamma1: Vector with the centred skewness parameter ("gamma1") estimates.

N: Number of observations.

CovCase: Configuration case of the variance-covariance matrix: Case 1 through Case 4

#### Methods

predict signature(object = "IdtSNlocda"): Classifies interval-valued observations in conjunction with snda.

show signature(object = "IdtSNlocda"): show S4 method for the IDdtlda-class

**CovCase** signature(object = "IdtSNlocda"): Returns the configuration case of the variance-covariance matrix

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

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### See Also

snda, MANOVA, IData

lda-methods

Linear Discriminant Analysis of Interval Data

## **Description**

lda performs linear discriminant analysis of Interval Data based on classic estimates of a mixture of Gaussian models.

### Usage

```
## S4 method for signature 'IData'
lda(x, grouping, prior="proportions", CVtol=1.0e-5, egvtol=1.0e-10,
    subset=1:nrow(x), CovCase=1:4, SelCrit=c("BIC","AIC"), silent=FALSE, k2max=1e6, ...)

## S4 method for signature 'IdtMxtNDE'
lda(x, prior="proportions", selmodel=BestModel(x), egvtol=1.0e-10,
    silent=FALSE, k2max=1e6, ...)

## S4 method for signature 'IdtClMANOVA'
lda( x, prior="proportions", selmodel=BestModel(H1res(x)),
    egvtol=1.0e-10, silent=FALSE, k2max=1e6, ...)

## S4 method for signature 'IdtLocNSNMANOVA'
lda( x, prior="proportions",
    selmodel=BestModel(H1res(x)@NMod), egvtol=1.0e-10, silent=FALSE, k2max=1e6, ...)
```

## **Arguments**

x	An object of class IData, IdtMxtNDE, IdtClMANOVA or IdtLocNSNMANOVA with either the original Interval Data, an estimate of a mixture of gaussian models for Interval Data, or the results of an Interval Data MANOVA, from which the discriminant analysis will be based.
grouping	Factor specifying the class for each observation.
prior	The prior probabilities of class membership. If unspecified, the class proportions for the training set are used. If present, the probabilities should be specified in the order of the factor levels.
CVtol	Tolerance level for absolute value of the coefficient of variation of non-constant variables. When a MidPoint or LogRange has an absolute value within-groups coefficient of variation below CVtol, it is considered to be a constant.
egvtol	Tolerance level for the eigenvalues of the product of the inverse within by the between covariance matrices. When a eigenvalue has an absolute value below egytol, it is considered to be zero.

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subset	An index vector specifying the cases to be used in the analysis.
CovCase	Configuration of the variance-covariance matrix: a set of integers between 1 and 4.
SelCrit	The model selection criterion.
silent	A boolean flag indicating whether a warning message should be printed if the method fails.
selmodel	Selected model from a list of candidate models saved in object x.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
	Other named arguments.

### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

#### See Also

```
qda, snda, Roblda, Robqda, IData, IdtMxtNDE, IdtClMANOVA, IdtLocNSNMANOVA, qda, ConfMat
```

### **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.
ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))</pre>
#Linear Discriminant Analysis
ChinaT.lda <- lda(ChinaT,ChinaTemp$GeoReg)</pre>
cat("Temperatures of China -- linear discriminant analysis results:\n")
print(ChinaT.lda)
ldapred <- predict(ChinaT.lda,ChinaT)$class</pre>
cat("lda Prediction results:\n")
print(ldapred )
cat("Resubstition confusion matrix:\n")
ConfMat(ChinaTemp$GeoReg,ldapred)
## Not run:
#Estimate error rates by ten-fold cross-validation replicated 20 times
CVlda <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=lda,CovCase=CovCase(ChinaT.lda))</pre>
summary(CVlda[,,"Clerr"])
```

## End(Not run)

LoansbyPurpose\_minmaxDt

Loans by purpose: minimum and maximum Data Set

### Description

This data set consist of the lower and upper bounds of the intervals for four interval characteristics of the loans aggregated by their purpose. The original microdata is available at the Kaggle Data Science platform and consists of 887 383 loan records characterized by 75 descriptors. Among the large set of variables available, we focus on borrowers' income and account and loan information aggregated by the 14 loan purposes, wich are considered as the units of interest.

#### Usage

data(LoansbyPurpose\_minmaxDt)

#### **Format**

A data frame containing 14 observations on the following 8 variables.

- **In-inc\_min** The minimum, for the current loan purpose, of natural logarithm of the self-reported annual income provided by the borrower during registration.
- **In-inc\_max** The maximum, for the current loan purpose, of natural logarithm of the self-reported annual income provided by the borrower during registration.
- **In-revolbal\_min** The minimum, for the current loan purpose, of natural logarithm of the total credit revolving balance.
- **In-revolbal\_max** The maximum, for the current loan purpose, of natural logarithm of the total credit revolving balance.
- **open-acc\_min** The minimum, for the current loan purpose, of the number of open credit lines in the borrower's credit file.
- **open-acc\_max** The maximum, for the current loan purpose, of the number of open credit lines in the borrower's credit file.
- **total-acc\_min** The minimum, for the current loan purpose, of the total number of credit lines currently in the borrower's credit file.
- **total-acc\_max** The maximum, for the current loan purpose, of the total number of credit lines currently in the borrower's credit file.

### Source

https:www.kaggle.com/wendykan/lending-club-loan-data

LoansbyRiskLvs\_minmaxDt

Loans by risk levels: minimum and maximum Data Set

## **Description**

This data set consist of the lower and upper bounds of the intervals for four interval characteristics for 35 risk levels (from A1 to G5) of loans. The original microdata is available at the Kaggle Data Science platform and consists of 887 383 loan records characterized by 75 descriptors. Among the large set of variables available, we focus on borrowers' income and account and loan information aggregated by the 35 risk levels wich are considered as the units of interest.

#### Usage

data(LoansbyRiskLvs\_minmaxDt)

#### **Format**

A data frame containing 35 observations on the following 8 variables.

- **In-inc\_min** The minimum, for the current risk category, of natural logarithm of the self-reported annual income provided by the borrower during registration.
- **In-inc\_max** The maximum, for the current risk category, of natural logarithm of the self-reported annual income provided by the borrower during registration.
- int-rate\_min The minimum, for the current risk category, of the interest rate on the loan.
- int-rate max The maximum, for the current risk category, of the interest rate on the loan.
- **open-acc\_min** The minimum, for the current risk category, of the number of open credit lines in the borrower's credit file.
- **open-acc\_max** The maximum, for the current risk category, of the number of open credit lines in the borrower's credit file.
- **total-acc\_min** The minimum, for the current risk category, of the total number of credit lines currently in the borrower's credit file.
- **total-acc\_max** The maximum, for the current risk category, of the total number of credit lines currently in the borrower's credit file.

#### Source

https://www.kaggle.com/wendykan/lending-club-loan-data

LoansbyRiskLvs\_qntlDt Loans by risk levels: ten and ninety per cent quantiles Data Set

### **Description**

This data set consist of the ten and ninety per cent quantiles of the intervals for four interval characteristics for 35 risk levels (from A1 to G5) of loans. The original microdata is available at the Kaggle Data Science platform and consists of 887 383 loan records characterized by 75 descriptors. Among the large set of variables available, we focus on borrowers' income and account and loan information aggregated by the 35 risk levels wich are considered as the units of interest.

#### Usage

data(LoansbyRiskLvs\_qntlDt)

#### **Format**

A data frame containing 35 observations on the following 8 variables.

- **ln-inc\_q0.10** The ten percent quantile, for the current risk category, of natural logarithm of the self-reported annual income provided by the borrower during registration.
- **In-inc\_q0.90** The ninety percent quantile, for the current risk category, of natural logarithm of the self-reported annual income provided by the borrower during registration.
- int-rate\_q0.10 The ten percent quantile, for the current risk category, of the interest rate on the loan.
- int-rate\_q0.90 The ninety percent quantile, for the current risk category, of the interest rate on the loan.
- open-acc\_q0.10 The ten percent quantile, for the current risk category, of the number of open credit lines in the borrower's credit file.
- open-acc\_q0.90 The ninety percent quantile, for the current risk category, of the number of open credit lines in the borrower's credit file.
- total-acc\_q0.10 The ten percent quantile, for the current risk category, of the total number of credit lines currently in the borrower's credit file.
- **total-acc\_q0.90** The ninety percent quantile, for the current risk category, of the total number of credit lines currently in the borrower's credit file.

#### Source

https://www.kaggle.com/wendykan/lending-club-loan-data

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LRTest-class

Class LRTest

## **Description**

LRTest contains the results of likelihood ratio tests

### **Slots**

ChiSq: Value of the Chi-Square statistics corresponding to the performed test

df: Degrees of freedom of the Chi-Square statistics

pvalue: p-value of the Chi-Square statistics value, obtained from the Chi-Square distribution with df degrees of freedom

H0logLik: Logarithm of the Likelihood function under the null hypothesis

H1logLik: Logarithm of the Likelihood function under the alternative hypothesis

#### Methods

show signature(object = "LRTest"): show S4 method for the LRTest-class

### Author(s)

Pedro Duarte Silva <psilva@porto.ucp.pt> Paula Brito <mpbrito.fep.up.pt>

#### See Also

mle, IData, ConfTests, MANOVA

MANOVA-methods

Methods for Function MANOVA in Package 'MAINT.Data'

# **Description**

Function MANOVA performs MANOVA tests based on likelihood ratios allowing for both Gaussian and Skew-Normal distributions and homoscedastic or heteroscedastic setups. Methods H0res and H1res retrieve the model estimates under the null and alternative hypothesis, and method show displays the MANOVA results.

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## Usage

## **Arguments**

object	An object representing a MANOVA analysis on interval-valued units.
Sdt	An IData object representing interval-valued units.
grouping	Factor indicating the group to which each observation belongs to.
Model	The joint distribution assumed for the MidPoint and LogRanges. Current alternatives are "Normal" for Gaussian distributions, "SKNormal" for Skew-Normal and "NrmandSKN" for both Gaussian and Skew-Normal distributions.
CovCase	Configuration of the variance-covariance matrix: a set of integers between 1 and 4.
SelCrit	The model selection criterion.
Mxt	Indicates the type of mixing distributions to be considered. Current alternatives are "Hom" (homoscedastic) and "Het" (heteroscedastic) for Gaussian models, "Loc" (location model – groups differ only on their location parameters) and "Gen" "Loc" (general model – groups differ on all parameters) for Skew-Normal models.
CVtol	Tolerance level for absolute value of the coefficient of variation of non-constant variables. When a MidPoint or LogRange has an absolute value within-groups coefficient of variation below CVtol, it is considered to be a constant.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
OptCntrl	List of optional control parameters to be passed to the optimization routine. See the documentation of RepLOptim for a description of the available options.
onerror	Indicates whether an error in the optimization algorithm should stop the current call, generate a warning, or return silently a NULL object.
	Other named arguments.

# Value

An object of class IdtMANOVA, containing the estimation and test results.

66 MANOVAPermTest

#### See Also

IdtMANOVA, RepLOptim

#### **Examples**

```
#Create an Interval-Data object containing the intervals of temperatures by quarter
# for 899 Chinese meteorological stations.
ChinaT <- IData(ChinaTemp[1:8])</pre>
#Classical (homoscedastic) MANOVA tests
ManvChina <- MANOVA(ChinaT,ChinaTemp$GeoReg)</pre>
cat("China, MANOVA by geografical regions results =\n")
print(ManvChina)
#Heteroscedastic MANOVA tests
HetManvChina <- MANOVA(ChinaT,ChinaTemp$GeoReg,Mxt="Het")</pre>
cat("China, heterocedastic MANOVA by geografical regions results =\n")
print(HetManvChina)
#Skew-Normal based MANOVA assuming the the groups differ only according to location parameters
## Not run:
SKNLocManvChina <- MANOVA(ChinaT,ChinaTemp$GeoReg,Model="SKNormal",Mxt="Loc")</pre>
cat("China, Skew-Normal MANOVA (location model) by geografical regions results =\n")
print(SKNLocManvChina)
#Skew-Normal based MANOVA assuming the the groups may differ in all parameters
SKNGenManvChina <- MANOVA(ChinaT,ChinaTemp$GeoReg,Model="SKNormal",Mxt="Gen")
cat("China, Skew-Normal MANOVA (general model) by geografical regions results =\n")
print(SKNGenManvChina)
## End(Not run)
```

### **Description**

MANOVAPermTest

Function MANOVAPermTest performs a MANOVA permutation test allowing for both Gaussian and Skew-Normal distributions and homoscedastic or heteroscedastic setups.

MANOVA permutation test

MANOVAPermTest 67

### Usage

```
MANOVAPermTest(MANOVAres, Sdt, grouping, nrep=200,
    Model=c("Normal","SKNormal","NrmandSKN"), CovCase=1:4,
    SelCrit=c("BIC","AIC"), Mxt=c("Hom","Het","Loc","Gen"), CVtol=1.0e-5, k2max=1e6,
    OptCntrl=list(), onerror=c("stop","warning","silentNull"), ...)
```

## **Arguments**

MANOVAres	An object representing a MANOVA analysis on interval-valued entities.
Sdt	An IData object representing interval-valued entities.
grouping	Factor indicating the group to which each observation belongs to.
nrep	Number of random generated permutations used to approximate the null distribution of the likelihood ratio statistic.
Model	The joint distribution assumed for the MidPoint and LogRanges. Current alternatives are "Normal" for Gaussian, distributions, "SKNormal" for Skew-Normal and "NrmandSKN" for both Gaussian and Skew-Normal distributions.
CovCase	Configuration of the variance-covariance matrix: a set of integers between 1 and 4.
SelCrit	The model selection criterion.
Mxt	Indicates the type of mixing distributions to be considered. Current alternatives are "Hom" (homocedastic) and "Het" (heteroscedastic) for Gaussian models, "Loc" (location model – groups differ only on their location parameters) and "Gen" "Loc" (general model – groups differ on all parameters) for Skew-Normal models.
CVtol	Tolerance level for absolute value of the coefficient of variation of non-constant variables. When a MidPoint or LogRange has an absolute value within-groups coefficient of variation below CVtol, it is considered to be a constant.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
OptCntrl	List of optional control parameters to passed to the optimization routine. See the documentation of RepLOptim for a description of the available options.
onerror	Indicates whether an error in the optimization algorithm should stop the current call, generate a warning, or return silently a NULL object.

# Details

Function MANOVAPermTest performs a MANOVA permutation test allowing for both Gaussian and Skew-Normal distributions and homoscedastic or heteroscedastic setups. This test is implemented by simulating the null distribution of the MANOVA likelihood ratio statistic, using many random permutations of the observation group labels. It is intended as an alternative of the classical

Other named arguments.

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Chi-squares based MANOVA likelihood ratio tests, when small sample sizes cast doubt on the applicability of the Chi-squared distribution. We note that this test may be computationally intensive, in particular when used for the Skw-Normal model.

#### Value

the p-value of the MANOVA permutation test.

#### See Also

MANOVA, IdtMANOVA

#### **Examples**

```
## Not run:
#Perform a MANOVA of the AbaloneIdt data set, comparing the Abalone variable means
# according to their age
# Create an Interval-Data object containing the Length, Diameter, Height, Whole weight,
# Shucked weight, Viscera weight (VW), and Shell weight (SeW) of 4177 Abalones,
# aggregated by sex and age.
# Note: The original micro-data (imported UCI Machine Learning Repository Abalone dataset)
# is given in the AbaDF data frame, and the corresponding values of the sex by age combinations
# is represented by the AbUnits factor.
AbaloneIdt <- AgrMcDt(AbaDF,AbUnits)
# Create a factor with three levels (Young, Adult and Old) for Abalones with respectively
# less than 10 rings, between 11 and 18 rings, and more than 18 rings.
Agestrg <- substring(rownames(AbaloneIdt),first=3)</pre>
AbalClass <- factor(ifelse(Agestrg=="1-3"|Agestrg=="4-6"| Agestrg=="7-9", "Young",
  ifelse(Agestrg=="10-12"|Agestrg=="13-15"| Agestrg=="16-18","Adult","Old") ) )
#Perform a classical MANOVA, computing the p-value from the asymptotic Chi-squared distribution
# of the Wilk's lambda statistic
MANOVAres <- MANOVA(AbaloneIdt,AbalClass)</pre>
summary(MANOVAres)
#Find a finite sample p-value of the test statistic, using a permutation test.
MANOVAPermTest(MANOVAres, AbaloneIdt, AbalClass)
## End(Not run)
```

mean–methods 69

mean--methods

Methods for function mean in Package 'MAINT.Data'

## **Description**

S4 methods for function mean. These methods extract estimates of mean vectors for the models fitted to Interval Data.

## Usage

```
## S4 method for signature 'IdtNDE'
mean(x)
## S4 method for signature 'IdtSNDE'
mean(x)
## S4 method for signature 'IdtNandSNDE'
mean(x)
## S4 method for signature 'IdtMxNDE'
mean(x)
## S4 method for signature 'IdtMxSNDE'
mean(x)
```

## **Arguments**

Х

An object representing a model fitted to interval data.

## Value

For the IdtNDE, IdtSNDE and IdtNandSNDE methods or IdtMxNDE, IdtMxSNDE methods with slot "Hmcdt" equal to TRUE: a matrix with the estimated correlations.

For the IdtMxNDE, and IdtMxSNDE methods with slot "Hmcdt" equal to FALSE: a three-dimensional array with a matrix with the estimated correlations for each group at each level of the third dimension.

### See Also

sd var cor

70 mle-methods

mle-methods Methods for function mle in Package 'MAINT.Data'	mle-methods	Methods for function mle in Package 'MAINT.Data'
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# Description

Performs maximum likelihood estimation for parametric models of interval data

## Usage

```
## S4 method for signature 'IData'
mle(Sdt, Model="Normal", CovCase="AllC", SelCrit=c("BIC","AIC"),
   k2max=1e6, OptCntrl=list(), ...)
```

## **Arguments**

Sdt	An IData object representing interval-valued units.
Model	The joint distribution assumed for the MidPoint and LogRanges. Current alternatives are "Normal" for Gaussian distributions, "SNNormal" for Skew-Normal and "NrmandSKN" for both Gaussian and Skew-Normal distributions.
CovCase	Configuration of the variance-covariance matrix: The string "AllC" for all possible configurations (default), or a set of integers between 1 and 4.
SelCrit	The model selection criterion.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
OptCntrl	List of optional control parameters to be passed to the optimization routine. See the documentation of RepLOptim for a description of the available options.
	Other named arguments.

### References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012): "Modelling Interval Data with Normal and Skew-Normal Distributions". Journal of Applied Statistics, Volume 39, Issue 1, 3-20.

## See Also

IData, RepLOptim

nycflights 71

### **Examples**

```
# Create an Interval-Data object containing the intervals of temperatures by quarter
# for 899 Chinese meteorological stations.

ChinaT <- IData(ChinaTemp[1:8])

# Estimate parameters by maximum likelihood assuming a Gaussian distribution

ChinaE <- mle(ChinaT)
cat("China maximum likelhiood estimation results =\n")
print(ChinaE)
cat("Standard Errors of Estimators:\n")
print(stdEr(ChinaE))</pre>
```

nycflights

New York City flights Data Set

## Description

A interval-valued data set containing 142 units and four interval-valued variables (dep\_delay, arr\_delay, air\_time and distance), created from from the flights data set in the R package nycflights13 (on-time data for all flights that departed the JFK, LGA or EWR airports in 2013), after removing all rows with missing observations, and aggregating by month and carrier.

### Usage

```
data(nycflights)
```

### **Format**

FlightsDF: A data frame containing the original 327346 valid (i.e. with non missing values) flights from the nycflights13 package, described by the 4 variables: dep\_delay, arr\_delay, air\_time and distance.

FlightsUnits: A factor with 327346 observations and 142 levels, indicating the month by carrier combination to which each original flight belongs to.

FlightsIdt: An IData object with 142 observations and 4 interval-valued variables, describing the intervals formed by agregating the FlightsDF microdata by the 0.05 and 0.95 quantiles of the subsamples formed by FlightsUnits factor.

72 pcoordplot-methods

pcoordplot-methods Parallel coordinates plot.	ncoordnlot-methods Parallel coordinates plot
---	--

### **Description**

Method poordplot displays a parallel coordinates plot, representing the results stored in an IdtMclust-method object.

### Usage

```
## S4 method for signature 'IdtMclust'
pcoordplot(x,title="Parallel Coordinate Plot",
Seq=c("AllMidP_AllLogR","MidPLogR_VarbyVar"), model ="BestModel", legendpar=list(), ...)
```

# **Arguments**

X	An object of type "IdtMclust" representing the the clusterig results of an Interval-

valued data set obtainde by the function "IdtMclust".

title The title of the plot.

Seq The ordering of the coordinates in the plot. Available options are:

"AllMidP\_AllLogR": all MidPoints followed all LogRanges, in the same vari-

able order.

"MidPLogR\_VarbyVar": MidPoints followed by LogRanges, variable by vari-

able.

model A character vector specifying the the model whose solution is to be displayed.

legendpar A named list with graphical parameters for the plot legend. Currently only the

base R 'cex.main' and 'cex.lab' parameters are implemented.

... Graphical arguments to be passed to methods

#### See Also

```
IdtMclust, Idtmclust, plotInfCrt
```

### **Examples**

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```
#Fit homoscedastic Gaussian mixtures with up to ten components
mclustres <- Idtmclust(LbyPIdt,G=1:10)
plotInfCrt(mclustres,legpos="bottomright")

#Display the results of the best mixture according to the BIC
pcoordplot(mclustres)
pcoordplot(mclustres,model="HomG6C1")
pcoordplot(mclustres,model="HomG4C1")

## End(Not run)</pre>
```

plot-methods

Methods for function plot in Package 'MAINT.Data'

## **Description**

S4 methods for function plot. As in the generic plot S3 'graphics' method, these methods plot Interval-valued data contained in IData objects.

# Usage

```
## S4 method for signature 'IData,IData'
plot(x, y, type=c("crosses","rectangles"), append=FALSE, ...)
## S4 method for signature 'IData,missing'
plot(x, casen=NULL, layout=c("vertical","horizontal"), append=FALSE, ...)
```

# Arguments

X	An object of type IData representing the values of an Interval-value variable.
У	An object of type IData representing the values of a second Interval-value variable, to be displayed along y (vertical) coordinates.
type	What type of plot should de drawn. Alternatives are "crosses" (default) and "rectangles".
append	A boolean flag indicating if the interval-valued variables should be displayed in a new plot, or added to an existing plot.
casen	An optional character string with the case names.
layout	The axes along which the interval-valued variables be displayed. Alternatives are "vertical" (default) and "horizontal".
	Graphical arguments to be passed to methods.

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## See Also

**IData** 

## **Examples**

```
## Not run:
 # Create an Interval-Data object containing the Length, Diameter, Height, Whole weight,
 # Shucked weight, Viscera weight (VW), and Shell weight (SeW) of 4177 Abalones,
 # aggregated by sex and age.
 # Note: The original micro-data (imported UCI Machine Learning Repository Abalone dataset)
 # is given in the AbaDF data frame, and the corresponding values of the sex by age combinations
 # is represented by the AbUnits factor.
 AbaloneIdt <- AgrMcDt(AbaDF,AbUnits)
 # Dispaly a plot of the Length versus the Whole_weight interval variables
 plot(AbaloneIdt[,"Length"],AbaloneIdt[,"Whole_weight"])
 plot(AbaloneIdt[,"Length"],AbaloneIdt[,"Whole_weight"],type="rectangles")
 # Display the Abalone lengths using different colors to distinguish the Abalones age
 # (measured by the number of rings)
 # Create a factor with three levels (Young, Adult and Old) for Abalones with
 # respectively less than 10 rings, between 11 and 18 rings, and more than 18 rings.
 Agestrg <- substring(rownames(AbaloneIdt), first=3)</pre>
 AbalClass <- factor(ifelse(Agestrg=="1-3"|Agestrg=="4-6"| Agestrg=="7-9","Young",
   ifelse(Agestrg=="10-12"|Agestrg=="13-15"| Agestrg=="16-18","Adult","Old") ) )
 plot(AbaloneIdt[AbalClass=="Young","Length"],col="blue",layout="horizontal")
 plot(AbaloneIdt[AbalClass=="Adult", "Length"], col="green", layout="horizontal", append=TRUE)
 plot(AbaloneIdt[AbalClass=="0ld","Length"],col="red",layout="horizontal",append=TRUE)
 legend("bottomleft",legend=c("Young","Adult","0ld"),col=c("blue","green","red"),lty=1)
 ## End(Not run)
plotInfCrt-methods
                         Information criteria plot.
```

## **Description**

Method plotInfCrt displays a plot representing the values of an appropriate information criterion (currently either BIC or AIC) for the models whose results are stored in an IdtMclust-method object. A supplementary short output message prints the values of the chosen criterion for the 'nprin' best models.

plotInfCrt-methods 75

## Usage

```
## S4 method for signature 'IdtMclust'
plotInfCrt(object, crt=object@SelCrit, legpos="right", nprnt=5,
  legendout=TRUE, outlegsize="adjstoscreen", outlegdisp="adjstoscreen",
  legendpar=list(), ...)
```

# **Arguments**

object	An object of type "IdtMclust" representing the the clusterig results of an Intervalvalued data set obtained by the function "IdtMclust".
crt	The information criteria whose values are to be displayed.
legpos	Legend position. Alternatives are "right" (default), "left", "bottomright", "bottomleft", "topright" and "topleft".
nprnt	Number of solutions for which the value of the information criterio should be printed in an suplmentary short output message.
legendout	A boolean flag indicating if the legend should be placed outside (default) or inside the main plot.
outlegsize	The size (in inches) to be reserved for a legend placed outside the main plot, or the string "adjstoscreen" (default) for an automatic adjustment of the plot and legend sizes.
outlegdisp	The displacement (as a percentage of the main plot size) of the outer margin for a legend placed outside the main plot, or the string "adjstoscreen" (default) for an automatic adjustment of the legend position.
legendpar	A named list with graphical parameters for the plot legend.

Graphical arguments to be passed to methods.

# See Also

. . .

IdtMclust, Idtmclust, pcoordplot

# **Examples**

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```
#Compare de model fit according to the BIC

plotInfCrt(mclustres,legpos="bottomleft")

#Display the results of the best three mixtures according to the BIC

summary(mclustres,parameters=TRUE,classification=TRUE)
pcoordplot(mclustres)
summary(mclustres,parameters=TRUE,classification=TRUE,model="HetG2C2")
summary(mclustres,parameters=TRUE,classification=TRUE,model="HomG6C1")
pcoordplot(mclustres,model="HomG6C1")

## End(Not run)
```

qda-methods

Quadratic Discriminant Analysis of Interval Data

#### **Description**

qda performs quadratic discriminant analysis of Interval Data based on classic estimates of a mixture of Gaussian models.

# Usage

```
## S4 method for signature 'IData'
qda( x, grouping, prior="proportions", CVtol=1.0e-5, subset=1:nrow(x),
    CovCase=1:4, SelCrit=c("BIC","AIC"), silent=FALSE, k2max=1e6, ... )

## S4 method for signature 'IdtMxtNDE'
qda(x, prior="proportions", selmodel=BestModel(x), silent=FALSE,
    k2max=1e6, ... )

## S4 method for signature 'IdtHetNMANOVA'
qda( x, prior="proportions", selmodel=BestModel(H1res(x)),
    silent=FALSE, k2max=1e6, ... )

## S4 method for signature 'IdtGenNSNMANOVA'
qda( x, prior="proportions",
    selmodel=BestModel(H1res(x)@NMod), silent=FALSE, k2max=1e6, ... )
```

## **Arguments**

Х

An object of class IData, IdtMxtNDE, IdtHetNMANOVA or IdtGenNSNMANOVA with either the original Interval Data, and estimate of a mixture of gaussian models for Interval Data, or the results of a Interval Data heterocedastic MANOVA, from which the discriminant analysis will be based.

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grouping	Factor specifying the class for each observation.
prior	The prior probabilities of class membership. If unspecified, the class proportions for the training set are used. If present, the probabilities should be specified in the order of the factor levels.
CVtol	Tolerance level for absolute value of the coefficient of variation of non-constant variables. When a MidPoint or LogRange has an absolute value within-groups coefficient of variation below CVtol, it is considered to be a constant.
subset	An index vector specifying the cases to be used in the analysis.
CovCase	Configuration of the variance-covariance matrix: a set of integers between 1 and 4.
SelCrit	The model selection criterion.
silent	A boolean flag indicating wether a warning message should be printed if the method fails.
selmodel	Selected model from a list of candidate models saved in object x.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
	Other named arguments.

#### References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. Journal of Applied Statistics 39(1), 3-20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

## See Also

lda, snda, Roblda, Robqda, IData, IdtMxtNDE, IdtHetNMANOVA, IdtGenNSNMANOVA, ConfMat

## **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.
ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))</pre>
#Quadratic Discriminant Analysis
ChinaT.qda <- qda(ChinaT,ChinaTemp$GeoReg)</pre>
cat("Temperatures of China -- qda discriminant analysis results:\n")
print(ChinaT.qda)
cat("Resubstition confusion matrix:\n")
ConfMat(ChinaTemp$GeoReg,predict(ChinaT.qda,ChinaT)$class)
## Not run:
```

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```
#Estimate error rates by ten-fold cross-validation replicated 20 times

CVqda <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=qda,CovCase=CovCase(ChinaT.qda))
summary(CVqda[,,"Clerr"])

## End(Not run)</pre>
```

qHardRoqF

Hardin and Rocke F-quantiles

## **Description**

p-quantiles of the Hardin and Rocke (2005) scaled F distribution for squared Mahalanobis distances based on raw MCD covariance estimators

## Usage

```
qHardRoqF(p, nobs, nvar, h=floor((nobs+nvar+1)/2), adj=TRUE,
lower.tail=TRUE, log.p=FALSE)
```

## **Arguments**

p	Vector of probabilities.
nobs	Number of observations used in the computation of the raw MCD Mahalanobis squared distances.
nvar	Number of variables used in the computation of the raw MCD Mahalanobis squared distances.
h	Number of observations kept in the computation of the raw MCD estimate.
adj	logical; if TRUE (default) returns the quantile of the adjusted distribution. Otherwise returns the quantile of the asymptotic distribution.
lower.tail	logical; if TRUE (default), probabilities are $P(X \le x)$ otherwise, $P(X > x)$
log.p	logical; if TRUE, probabilities p are given as log(p).

# Value

The quantile of the appropriate scaled F distribution.

## References

Hardin, J. and Rocke, A. (2005), The Distribution of Robust Distances. *Journal of Computational and Graphical Statistics* **14**, 910–927.

#### See Also

fasttle, fulltle

RepLOptim 79

RepLOptim	Repeated Local Optimization	
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# Description

'RepLOptim' Tries to minimize a function calling local optimizers several times from different random starting points.

# Usage

```
RepLOptim(start, parsd, fr, gr=NULL, inphess=NULL, ..., method="nlminb",
lower=NULL, upper=NULL, rethess=FALSE, parmstder=FALSE, control=list())
```

# Arguments

start	Vector of starting points used in the first call of the local optimizer.
parsd	Vector of standard deviations for the parameter distribution generating starting points for the local optimizer.
fr	The function to be minimized. If method is neither "nlminb" or "L-BFGS-B", fr should accept a lbound and an ubound arguments for the parameter bounds, and should enforce these bounds before calling the local optimization routine.
gr	A function to return the gradient for the "nlminb", "BFGS", "CG" and L-BFGS-B methods. If it is 'NULL', a finite-difference approximation will be used. For the "SANN" method it specifies a function to generate a new candidate point. If it is 'NULL' a default Gaussian Markov kernel is used.
inphess	A function to return the hessian for the "nlminb" method. Must return a square matrix of order 'length(parmean)' with the different hessian elements in its lower triangle. It is ignored if method component of the control list is not set to its "nlminb" default.
	Further arguments to be passed to 'fr', 'gr' and 'inphess'.
method	The method to be used. See 'Details'.
lower	Vector of parameter lower bounds. Set to '-Inf' (no bounds) by default.
upper	Vector of parameter upper bounds. Set to 'Inf' (no bounds) by default.
rethess	Boolean flag indicating whether a numerically evaluated hessian matrix at the optimum should be computed and returned. Not available for the "nlminb" method.
parmstder	Boolean flag indicating whether parameter assymptotic standard errors based on the inverse hessian approximation to the Fisher information matrix should be computed and returned. Only available if hessian is set to TRUE and if a local miminum with a positive-definite hessian was indeed found. This requirement may fail if 'nrep' and 'niter' (and maybe 'neval') are not large enough, and for non-trivial problems of moderate or high dimensionality may never be satisfied because of numerical difficulties.
control	A list of control parameters. See below for details.

#### **Details**

'RepLOptim' Tries to minimize a function by calling local optimizers several times from different starting points. The starting point used in the first call the local optimizer is the value of the argument 'start'. Subsquent calls use starting points generated from uniform distributions of independent variates with means equal to the current best parameter values and standard deviations equal to the values of the argument 'parsd'. If parameter bounds are specified and the uniform limits implied by 'parsd' violate those bounds, these limits are replaced by the corresponding bounds.

The choice of the local optimizer is made by value of the 'method' argument. This argument can be a function object implementing the optimizer or a string describing an available R method. In the latter case current alternatives are: "nlminb" (default) for the 'nlminb' port routine, "nlm" for the 'nlm' function and "Nelder-Mead", "L-BFGS-B", "CG", "L-BFGS-B" and "SANN" for the corresponding methods of the 'optim' function.

Arguments for controling the behaviour of the local optimizer can be specified as components of control list. This list can include any of the following components:

- **maxrepet** Maximum time of repetions of the same minimum objective value, before RepLOptim is stoped and the current best solution is returned. By default set to 2.
- **maxnoimprov** Maximum number of times the local optimizer is called without improvements in the minimum objective value, before RepLOptim is stopped and the current best solution is returned. By default set to 50.
- **maxreplic** Maximum number of times the local optimizer is called and returns a valid solution before RepLOptim is stoped and the current best solution is returned. By default set to 250.
- **allrep** Total maximum number of replications (including those leading to non-valid solutions) performed. By default equals ten times the value of maxreplic. Ignored when objbnd is set to 'Inf'.
- **maxiter** Maximum number of iterations performed in each call to the local optimizer. By default set to 500 except with the "SANN" mehtod, when by default is set to 1500.
- **maxeval** Maximum number of function evaluations (nlminb method only) performed in each call to the nlminb optimizer. By defaults set to 1000.
- **RLOtol** The relative convergence tolerance of the local optimizer. The local optimizer stops if it is unable to reduce the value by a factor of 'RLOtol \*(abs(val) + reltol)' at a step. Ignored when method is set to "nlm". By default set to the square root of the computer precision, i.e. to 'sqrt(.Machine\$double.eps)'.
- **HesEgtol** Numerical tolerance used to ensure that the hessian is non-singular. If the last eigenvalue of the hessian is positive but the ratio between it and the first eigenvalue is below HesEgtol the hessian is considered to be semi-definite and the parameter assymptotic standard errors are not computed. By default set to the square root of the computer precision, i.e. to 'sqrt(.Machine\$double.eps)'.
- **objbnd** Upper bound for the objective. Only solutions leading to objective values below objbnd are considered as valid.

#### Value

A list with the following components:

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par	The best result found for the parameter vector.
val	The best value (minimum) found for the function fr.
vallist	A vector with the best values found for each starting point.
iterations	Number the iterations performed by the local optimizer in the call that generated the best result.
vallis	A vector with the best values found for each starting point.
counts	number of times the function fr was evaluated in the call that generated the result returned.
convergence	Code with the convergence status returned by the local optimizer.
message	Message generated by the local optimizer.
hessian	Numerically evaluated hessian of fr at the result returned. Only returned when the parameter hessian is set to TRUE.
hessegval	Eigenvalues of the hessian matrix. Used to confirm if a local minimum was indeed found. Only returned when the parameter hessian is set to TRUE.
stderrors	Assymptotic standard deviations of the parameters based on the observed information matrix. Only returned when the parse parameter is set to true and the hessian is indeed positive definite.

# Author(s)

A. Pedro Duarte Silva

Robda-methods	Robust Discriminant Analysis of Interval Data

## **Description**

Roblda and Robqda perform linear and quadratic discriminant analysis of Interval Data based on robust estimates of location and scatter.

# Usage

```
## S4 method for signature 'IData'
Roblda( x, grouping, prior="proportions", CVtol=1.0e-5, egvtol=1.0e-10,
    subset=1:nrow(x), CovCase=1:4, SelCrit=c("BIC","AIC"), silent=FALSE,
    CovEstMet=c("Pooled","Globdev"), SngDMet=c("fasttle","fulltle"), k2max=1e6,
    Robcontrol=RobEstControl(), ... )

## S4 method for signature 'IData'
Robqda( x, grouping, prior="proportions", CVtol=1.0e-5,
    subset=1:nrow(x), CovCase=1:4, SelCrit=c("BIC","AIC"), silent=FALSE,
    SngDMet=c("fasttle","fulltle"), k2max=1e6, Robcontrol=RobEstControl(), ... )
```

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## **Arguments**

An object of class IData with the original Interval Data. Factor specifying the class for each observation. grouping The prior probabilities of class membership. If unspecified, the class proportions prior for the training set are used. If present, the probabilities should be specified in the order of the factor levels. CVtol Tolerance level for absolute value of the coefficient of variation of non-constant variables. When a MidPoint or LogRange has an absolute value within-groups coefficient of variation below CVtol, it is considered to be a constant. Tolerance level for the eigenvalues of the product of the inverse within by the egvtol between covariance matrices. When a eigenvalue has an absolute value below egytol, it is considered to be zero. subset An index vector specifying the cases to be used in the analysis. CovCase Configuration of the variance-covariance matrix: a set of integers between 1 and SelCrit The model selection criterion. A boolean flag indicating wether a warning message should be printed if the silent method fails. CovEstMet Method used to estimate the common covariance matrix in Roblda (Robust linear discriminant analysis). Alternatives are "Pooled" (default) for a pooled average of the the robust within-groups covariance estimates, and "Globdev" for a global estimate based on all deviations from the groups multivariate 1 1 medians. See Todorov and Filzmoser (2009) for details. SngDMet Algorithm used to find the robust estimates of location and scatter. Alternatives are "fasttle" (default) and "fulltle". Maximal allowed 12-norm condition number for correlation matrices. Correlak2max tion matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results. Robcontrol A control object (S4) of class RobEstControl-class containing estimation options - same as these provided in the function specification. If the control object is supplied, the parameters from it will be used. If parameters are passed also in the invocation statement, they will override the corresponding elements of the control object. Other named arguments.

## References

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

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#### See Also

lda, qda, snda, IData, RobEstControl,codeConfMat

## **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
 # on the temperatures by quarter in 60 Chinese meteorological stations.
 ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))</pre>
 #Robust Linear Discriminant Analysis
 ## Not run:
 ChinaT.rlda <- Roblda(ChinaT,ChinaTemp$GeoReg)</pre>
 cat("Temperatures of China -- robust lda discriminant analysis results:\n")
 print(ChinaT.rlda)
 cat("Resubstition confusion matrix:\n")
 ConfMat(ChinaTemp$GeoReg,predict(ChinaT.rlda,ChinaT)$class)
 #Estimate error rates by ten-fold cross-validation with 5 replications
 CVrlda <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=Roblda,CovCase=CovCase(ChinaT.rlda),
    CVrep=5)
 summary(CVrlda[,,"Clerr"])
 #Robust Quadratic Discriminant Analysis
 ChinaT.rgda <- Robgda(ChinaT,ChinaTemp$GeoReg)</pre>
 cat("Temperatures of China -- robust qda discriminant analysis results:\n")
 print(ChinaT.rqda)
 cat("Resubstition confusion matrix:\n")
 ConfMat(ChinaTemp$GeoReg,predict(ChinaT.rqda,ChinaT)$class)
 #Estimate error rates by ten-fold cross-validation with 5 replications
 CVrqda <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=Robqda,CovCase=CovCase(ChinaT.rqda),</pre>
    CVrep=5)
 summary(CVrqda[,,"Clerr"])
 ## End(Not run)
RobEstControl
                          Constructor function for objects of class RobEstControl
```

#### Description

This function will create a control object of class RobEstControl containing the control parameters for the robust estimation functions fasttle, RobMxtDEst, Roblda and Robqda.

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## Usage

RobEstControl(alpha=0.75, nsamp=500, seed=NULL, trace=FALSE, use.correction=TRUE, ncsteps=200, getalpha="TwoStep", rawMD2Dist="ChiSq", MD2Dist="ChiSq", eta=0.025, multiCmpCor="never", getkdblstar="Twopplusone", outlin="MidPandLogR", trialmethod="simple", m=1, reweighted=TRUE, k2max=1e6, otpType="SetMD2andEst")

#### **Arguments**

alpha Numeric parameter controlling the size of the subsets over which the trimmed

likelihood is maximized; roughly alpha\*nrow(Sdt) observations are used for computing the trimmed likelihood. Allowed values are between 0.5 and 1. Note that when argument 'getalpha' is set to "TwoStep" the final value of 'alpha' is estimated by a two-step procedure and the value of argument 'alpha' is only

used to specify the size of the samples used in the first step.

nsamp Number of subsets used for initial estimates.

seed Starting value for random generator.
trace Whether to print intermediate results.

use.correction Whether to use finite sample correction factors.

ncsteps The maximum number of concentration steps used each iteration of the fasttle

algorithm.

getalpha Argument specifying if the 'alpha' parameter (roughly the percentage of the

sample used for computing the trimmed likelihood) should be estimadted from the data, or if the value of the argument 'alpha' should be used instead. When set to "TwoStep", 'alpha' is estimated by a two-step procedure with the value of argument 'alpha' specifying the size of the samples used in the first step.

Otherwise the value of argument 'alpha' is used directly.

rawMD2Dist The assumed reference distribution of the raw MCD squared distances, which is

used to find to cutoffs defining the observations kept in one-step reweighted MCD estimates. Alternatives are 'ChiSq', 'HardRockeAsF' and 'HardRockeAdjF', respectively for the usual Chi-squared, and the asymptotic and adjusted

scaled F distributions proposed by Hardin and Rocke (2005).

MD2Dist The assumed reference distributions used to find cutoffs defining the observa-

tions assumed as outliers. Alternatives are "ChiSq" and "CerioliBetaF" respectivelly for the usual Chi-squared, the Beta and F distributions proposed by Ceri-

oli (2010).

eta Nominal size of the null hypothesis that a given observation is not an outlier.

Defines the raw MCD Mahalanobis distances cutoff used to choose the observa-

tions kept in the reweightening step.

multiCmpCor Whether a multicomparison correction of the nominal size (eta) for the outliers

tests should be performed. Alternatives are: 'never' – ignoring the multicomparisons and testing all entities at 'eta'. 'always' – testing all n entities at 1.-(1.-'eta'^(1/n)); and 'iterstep' – as sugested by Cerioli (2010), make an initial set of tests using the nominal size 1.- (1-'eta'^(1/n)), and if no outliers were

detected stop. Otherwise, make a second step testing for outliers at 'eta'.

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getkdblstar Argument specifying the size of the initial small (in order to minimize the prob-

ability of outliers) subsets. If set to the string "Twopplusone" (default) the initial sets have twice the number of interval-value variables plus one which are they are the smaller samples that lead to a non-singular covaraince estimate). Other-

wise, an integer with the size of the initial sets.

outlin The type of outliers to be considered. "MidPandLogR" if outliers may be present

in both MidPpoints and LogRanges, "MidP" if outliers are only present in MidP-

points, or "LogR" if outliers are only present in LogRanges.

trialmethod The method to find a trial subset used to initialize each replication of the fasttle

algorithm. The current options are "simple" (default) that simply selects 'kd-blstar' observations at random, and "Poolm" that divides the original sample into 'm' non-overlaping subsets, applies the 'simple trial' and the refinement

methods to each one of them, and merges the results into a trial subset.

m Number of non-overlaping subsets used by the trial method when the argument

of 'trialmethod' is set to 'Poolm'.

reweighted Should a (Re)weighted estimate of the covariance matrix be used in the compu-

tation of the trimmed likelihood or just a "raw" covariance estimate; default is

(Re)weighting.

k2max Maximal allowed 12-norm condition number for correlation matrices. Correla-

tion matrices with condition number above k2max are considered to be numeri-

cally singular, leading to degenerate results.

otpType The amount of output returned by fasttle.

Current options are "SetMD2andEst" (default) which returns an 'IdtSngNDRE' object with the fasttle estimates, a vector with the final trimmed subset elements used to compute these estimates and the corresponding robust squared Mahalanobis distances, and "SetMD2EstandPrfSt" wich returns an 'IdtSngNDRE' object with the previous slots plust a list of some performance statistics con-

cerning the algorithm execution.

## Value

A RobEstControl object

## References

Brito, P., Duarte Silva, A. P. (2012): "Modelling Interval Data with Normal and Skew-Normal Distributions". Journal of Applied Statistics, Volume 39, Issue 1, 3-20.

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. *Journal of the American Statistical Association* **105** (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Hardin, J. and Rocke, A. (2005), The Distribution of Robust Distances. *Journal of Computational and Graphical Statistics* **14**, 910–927.

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Todorov V. and Filzmoser P. (2009), An Object Oriented Framework for Robust Multivariate Analysis. *Journal of Statistical Software* **32**(3), 1–47.

#### See Also

RobEstControl, fasttle, RobMxtDEst, Roblda, Robqda

RobEstControl-class

Class 'RobEstControl' - contains control parameters for the robust estimation of parametric interval data models.

## **Description**

This class extends the CovControlMcd class and contains control parameters for the robust estimation of parametric interval data models.

## **Objects from the Class**

Objects can be created by calls of the form new("RobEstControl", ...) or by calling the constructorfunction RobEstControl.

#### **Slots**

alpha: Inherited from class "CovControlMcd". Numeric parameter controlling the size of the subsets over which the trimmed likelihood is maximized; roughly alpha\*nrow(Sdt) observations are used for computing the trimmed likelihood. Allowed values are between 0.5 and 1. Note that when argument 'getalpha' is set to "TwoStep" the final value of 'alpha' is estimated by a two-step procedure and the value of argument 'alpha' is only used to specify the size of the samples used in the first step.

nsamp: Inherited from class "CovControlMcd". Number of subsets used for initial estimates.

scalefn: Inherited from class "CovControlMcd" and not used in the package 'Maint.Data.'

maxcsteps: Inherited from class "CovControlMcd" and not used in the package 'Maint.Data.'

seed: Inherited from class "CovControlMcd". Starting value for random generator. Default is seed = NULL.

use.correction: Inherited from class "CovControlMcd". Whether to use finite sample correction factors. Default is use.correction=TRUE.

trace, tolSolve: Inherited from class "CovControl".

ncsteps: The maximum number of concentration steps used each iteration of the fasttle algorithm.

getalpha: Argument specifying if the 'alpha' parameter (roughly the percentage of the sample used for computing the trimmed likelihood) should be estimated from the data, or if the value of the argument 'alpha' should be used instead. When set to "TwoStep", 'alpha' is estimated by a two-step procedure with the value of argument 'alpha' specifying the size of the samples used in the first step. Otherwise, with the value of argument 'alpha' is used directly.

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rawMD2Dist: The assumed reference distribution of the raw MCD squared distances, which is used to find to cutoffs defining the observations kept in one-step reweighted MCD estimates. Alternatives are 'ChiSq', 'HardRockeAsF' and 'HardRockeAdjF', respectively for the usual Chi-squared, and the asymptotic and adjusted scaled F distributions proposed by Hardin and Rocke (2005).

- MD2Dist: The assumed reference distributions used to find cutoffs defining the observations assumed as outliers. Alternatives are "ChiSq" and "CerioliBetaF" respectively for the usual Chi-squared, and the Beta and F distributions proposed by Cerioli (2010).
- eta: Nominal size of the null hypothesis that a given observation is not an outlier. Defines the raw MCD Mahalanobis distances cutoff used to choose the observations kept in the reweightening step.
- multiCmpCor: Whether a multicomparison correction of the nominal size (eta) for the outliers tests should be performed. Alternatives are: 'never' ignoring the multicomparisons and testing all entities at 'eta'. 'always' testing all n entitites at 1.- (1.-'eta'^(1/n)); and 'iterstep' as suggested by Cerioli (2010), make an initial set of tests using the nominal size 1.- (1-'eta'^(1/n)), and if no outliers were detected stop. Otherwise, make a second step testing for outliers at 'eta'.
- getkdblstar: Argument specifying the size of the initial small (in order to minimize the probability of outliers) subsets. If set to the string "Twopplusone" (default) the initial sets have twice the number of interval-value variables plus one (i.e., they are the smaller samples that lead to a non-singular covariance estimate). Otherwise, an integer with the size of the initial sets.
- k2max: Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
- outlin: The type of outliers to be consideres. "MidPandLogR" if outliers may be present in both MidPpoints and LogRanges, "MidP" if outliers are only present in MidPpoints, or "LogR" if outliers are only present in LogRanges.
- trialmethod: The method to find a trial subset used to initialize each replication of the fasttle algorithm. The current options are "simple" (default) that simply selects 'kdblstar' observations at random, and "Poolm" that divides the original sample into 'm' non-overlaping subsets, applies the 'simple trial' and the refinement methods to each one of them, and merges the results into a trial subset.
- m: Number of non-overlaping subsets used by the trial method when the argument of 'trialmethod' is set to 'Poolm'.
- reweighted: Should a (Re)weighted estimate of the covariance matrix be used in the computation of the trimmed likelihood or just a "raw" covariance estimate; default is (Re)weighting.
- otpType: The amount of output returned by fasttle. Current options are "OnlyEst" (default) where only an 'IdtE' object with the fasttle estimates is returned, "SetMD2andEst" which returns a list with an 'IdtE' object of fasttle estimates, a vector with the final trimmed subset elements used to compute these estimates and the corresponding robust squared Mahalanobis distances, and "SetMD2EstandPrfSt" wich returns a list with the previous three components plust a list of some performance statistics concerning the algorithm execution.

## **Extends**

Class CovControlMcd, directly. Class CovControl by CovControlMcd, distance 2.

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#### Methods

No methods defined with class "RobEstControl" in the signature.

#### References

Cerioli, A. (2010), Multivariate Outlier Detection with High-Breakdown Estimators. *Journal of the American Statistical Association* **105** (489), 147–156.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Hardin, J. and Rocke, A. (2005), The Distribution of Robust Distances. *Journal of Computational and Graphical Statistics* **14**, 910–927.

Todorov V. and Filzmoser P. (2009), An Object Oriented Framework for Robust Multivariate Analysis. *Journal of Statistical Software* **32**(3), 1–47.

#### See Also

RobEstControl, fasttle, RobMxtDEst, Roblda, Robqda

RobMxtDEst-methods

Methods for Function RobMxtDEst in Package 'MAINT.Data'

#### **Description**

RobMxtDEst estimates mixtures of distribution for interval-valued data using robust methods.

## Usage

## **Arguments**

Sdt An IData object representing interval-valued entities.

grouping Factor indicating the group to which each observation belongs to.

Mxt Indicates the type of mixing distributions to be considered. Current alternatives

are "Hom" (homocedastic) and "Het" (hetereocedasic).

CovEstMet Method used to estimate the common covariance matrix. Alternatives are "Pooled"

(default) for a pooled average of the the robust within-groups covariance estimates, and "Globdev" for a global estimate based on all deviations from the

groups multivariate 1\_1 medians.

See Todorov and Filzmoser (2009) for details..

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CovCase Configuration of the variance-covariance matrix: a set of integers between 1 and

4.

SelCrit The model selection criterion.

Robcontrol A control object (S4) of class RobEstControl-class containing estimation op-

tions - same as these provided in the function specification. If the control object is supplied, the parameters from it will be used. If parameters are passed also in the invocation statement, they will override the corresponding elements of the

control object.

11medpar List of named arguments to be passed to the function pcaPP::11median (in

package pcaPP) used to find the multivariate l\_1 medians. Possible components are 'MaxStep', 'ItTol' and 'trace' (see the documentation of pcaPP::l1median

for details).

If kept at NULL (default) the defaults of pcaPP::11median will be used.

... Other named arguments.

#### Value

An object of class IdtMxNDRE, containing the estimation results.

## References

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P., Filzmoser, P. and Brito, P. (2017), Outlier detection in interval data. *Advances in Data Analysis and Classification*, 1–38.

Todorov V. and Filzmoser P. (2009), An Object Oriented Framework for Robust Multivariate Analysis. *Journal of Statistical Software* **32**(3), 1–47.

#### See Also

IdtMxNDRE, RobEstControl.

# **Examples**

```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.

ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))

## Not run:

# Estimate robustly an homoscedastic mixture, with mixture components defined by regions

ChinaHomMxtRobE <- RobMxtDEst(ChinaT, ChinaTemp$GeoReg)

print(ChinaHomMxtRobE)</pre>
```

# Estimate robustly an heteroscedastic mixture, with mixture components defined by regions

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```
ChinaHetMxtRobE <- RobMxtDEst(ChinaT,ChinaTemp$GeoReg,Mxt="Het")
print(ChinaHetMxtRobE)
## End(Not run)</pre>
```

snda-methods

Skew-Normal Discriminant Analysis of Interval Data

#### **Description**

snda performs discriminant analysis of Interval Data based on estimates of mixtures of Skew-Normal models

## Usage

```
## S4 method for signature 'IData'
snda(x, grouping, prior="proportions", CVtol=1.0e-5, subset=1:nrow(x),
    CovCase=1:4, SelCrit=c("BIC","AIC"), Mxt=c("Loc","Gen"), k2max=1e6, ... )

## S4 method for signature 'IdtLocSNMANOVA'
snda( x, prior="proportions", selmodel=BestModel(H1res(x)),
    egvtol=1.0e-10, silent=FALSE, k2max=1e6, ... )

## S4 method for signature 'IdtLocNSNMANOVA'
snda( x, prior="proportions",
    selmodel=BestModel(H1res(x)@SNMod), egvtol=1.0e-10, silent=FALSE, k2max=1e6, ... )

## S4 method for signature 'IdtGenSNMANOVA'
snda( x, prior="proportions", selmodel=BestModel(H1res(x)),
    silent=FALSE, k2max=1e6, ... )

## S4 method for signature 'IdtGenNSNMANOVA'
snda( x, prior="proportions",
    selmodel=BestModel(H1res(x)@SNMod), silent=FALSE, k2max=1e6, ... )
```

#### **Arguments**

x An object of class IData, IdtLocSNMANOVA, IdtLocNSNMANOVA, IdtGenSNMANOVA

or IdtGenNSNMANOVA with either the original Interval Data, or the results of a Interval Data Skew-Normal MANOVA, from which the discriminant analysis

will be based.

grouping Factor specifying the class for each observation.

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prior	The prior probabilities of class membership. If unspecified, the class proportions for the training set are used. If present, the probabilities should be specified in the order of the factor levels.
CVtol	Tolerance level for absolute value of the coefficient of variation of non-constant variables. When a MidPoint or LogRange has an absolute value within-groups coefficient of variation below CVtol, it is considered to be a constant.
subset	An index vector specifying the cases to be used in the analysis.
CovCase	Configuration of the variance-covariance matrix: a set of integers between 1 and 4.
SelCrit	The model selection criterion.
Mxt	Indicates the type of mixing distributions to be considered. Current alternatives are "Loc" (location model – groups differ only on the location parameters of a Skew-Normal model) and "Gen" (general model – groups differ on all parameters of a Skew-Normal models).
silent	A boolean flag indicating whether a warning message should be printed if the method fails.
selmodel	Selected model from a list of candidate models saved in object x.
egvtol	Tolerance level for the eigenvalues of the product of the inverse within by the between covariance matrices. When a eigenvalue has an absolute value below egytol, it is considered to be zero.
k2max	Maximal allowed 12-norm condition number for correlation matrices. Correlation matrices with condition number above k2max are considered to be numerically singular, leading to degenerate results.
	Other named arguments.

## References

Azzalini, A. and Dalla Valle, A. (1996), The multivariate skew-normal distribution. *Biometrika* **83**(4), 715–726.

Brito, P., Duarte Silva, A. P. (2012), Modelling Interval Data with Normal and Skew-Normal Distributions. *Journal of Applied Statistics* **39**(1), 3–20.

Duarte Silva, A.P. and Brito, P. (2015), Discriminant analysis of interval data: An assessment of parametric and distance-based approaches. *Journal of Classification* **39**(3), 516–541.

## See Also

 $\label{locnsnmanova} Ida, qda, Roblda, Robqda, IData, IdtLocSNMANOVA, IdtLocNSNMANOVA, IdtGenSNMANOVA, IdtGe$ 

# **Examples**

## Not run:

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```
# Create an Interval-Data object containing the intervals for 899 observations
# on the temperatures by quarter in 60 Chinese meteorological stations.
ChinaT <- IData(ChinaTemp[1:8], VarNames=c("T1", "T2", "T3", "T4"))</pre>
# Skew-Normal based discriminant analysis, asssuming that the different regions differ
# only in location parameters
ChinaT.locsnda <- snda(ChinaT,ChinaTemp$GeoReg,Mxt="Loc")</pre>
cat("Temperatures of China -- SkewNormal location model discriminant analysis results:\n")
print(ChinaT.locsnda)
cat("Resubstition confusion matrix:\n")
ConfMat(ChinaTemp$GeoReg,predict(ChinaT.locsnda,ChinaT)$class)
#Estimate error rates by three-fold cross-validation without replication
CVlocsnda <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=snda,Mxt="Loc",</pre>
 CovCase=CovCase(ChinaT.locsnda),kfold=3,CVrep=1)
summary(CVlocsnda[,,"Clerr"])
# Skew-Normal based discriminant analysis, asssuming that the different regions may differ
# in all SkewNormal parameters
ChinaT.gensnda <- snda(ChinaT,ChinaTemp$GeoReg,Mxt="Gen")</pre>
cat("Temperatures of China -- SkewNormal general model discriminant analysis results:\n")
print(ChinaT.gensnda)
cat("Resubstition confusion matrix:\n")
ConfMat(ChinaTemp$GeoReg,predict(ChinaT.gensnda,ChinaT)$class)
#Estimate error rates by three-fold cross-validation without replication
CVgensnda <- DACrossVal(ChinaT,ChinaTemp$GeoReg,TrainAlg=snda,Mxt="Gen",</pre>
 CovCase=CovCase(ChinaT.gensnda),kfold=3,CVrep=1)
summary(CVgensnda[,,"Clerr"])
## End(Not run)
```

stdEr--methods

Methods for function stdEr in Package 'MAINT.Data'

#### **Description**

S4 methods for function stdEr. As in the generic stdEr S3 'miscTools' method, these methods extract standard errors of the parameter estimates, for the models fitted to Interval Data.

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## Usage

```
## S4 method for signature 'IdtNDE'
stdEr(x, selmodel=BestModel(x), ...)
## S4 method for signature 'IdtSNDE'
stdEr(x, selmodel=BestModel(x), ...)
## S4 method for signature 'IdtNandSNDE'
stdEr(x, selmodel=BestModel(x), ...)
```

#### **Arguments**

x An object representing a model fitted to interval data.

selmodel Selected model from a list of candidate models saved in object x.

... Additional arguments for method functions.

#### Value

A vector of the estimated standard deviations of the parameter estimators.

#### See Also

vcov

summary-methods IdtMclust summary method

## **Description**

summary methods for the classe IdtMclust defined in Package 'MAINT.Data'.

# Usage

```
## S4 method for signature 'IdtMclust'
summary(object, parameters = FALSE, classification = FALSE, model = "BestModel",
ShowClassbyOBs = FALSE, ...)
```

## **Arguments**

object An object of class IdtMclust representing the results of fitting Gaussian mix-

tures to interval data objects

parameters A boolean flag indicating if the parameter estimates of the optimal mixture

should be displayed

classification A boolean flag indicating if the crisp classification resulting from the optimal

mixture should be displayed

model A character vector specifying the the model whose solution is to be displayed.

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ShowClassbyOBs A boolean flag indicating if class membership should shown by observation or by class (default).

Other named arguments.

## See Also

Idtmclust, IdtMclust, plotInfCrt, pcoordplot

testMod-methods	Methods for Function testMod in Package 'MAINT.Data'	
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## **Description**

Performs statistical likelihood-ratio tests that evaluate the goodness-of-fit of a nested model against a more general one.

# Usage

testMod(ModE,RestMod=ModE@ModelConfig[2]:length(ModE@ModelConfig),FullMod="Next")

# **Arguments**

ModE	An object of class IdtE representing the estimates of a model fitted to a data set

of interval-value variables

RestMod Indices of the restricted models being evaluated in the NULL hypothesis

FullMod Either indices of the general models being evaluated in the alternative hypothesis

or the strings "Next" (default) or "All". In the former case a Restricted model is always compared against the most parsimonious alternative that encompasses

it, and in latter all possible comparisons are performed

## Value

An object of class ConfTests with the results of the tests performed

## **Examples**

```
# Create an Interval-Data object containing the intervals of temperatures by quarter
# for 899 Chinese meteorological stations.

ChinaT <- IData(ChinaTemp[1:8])

# Estimate by maximum likelihood the parameters of Gaussian models
# for the Winter (1st and 4th) quarter intervals

ChinaWTE <- mle(ChinaT[,c(1,4)])
cat("China maximum likelihood estimation results for Winter quarters:\n")
print(ChinaWTE)</pre>
```

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```
# Perform Likelihood-Ratio tests comparing models with consecutive nested Configuration
testMod(ChinaWTE)

# Perform Likelihood-Ratio tests comparing all possible models
testMod(ChinaWTE,FullMod="All")

# Compare model with covariance Configuration case 3 (MidPoints independent of LogRanges)
# against model with covariance Configuration 1 (unrestricted covariance)
testMod(ChinaWTE,RestMod=3,FullMod=1)
```

var--methods

Methods for function var in Package 'MAINT.Data'

# **Description**

S4 methods for function var. These methods extract estimates of variance-covariance matrices for the models fitted to Interval Data.

## Usage

```
## S4 method for signature 'IdtNDE'
var(x)
## S4 method for signature 'IdtSNDE'
var(x)
## S4 method for signature 'IdtNandSNDE'
var(x)
## S4 method for signature 'IdtMxNDE'
var(x)
## S4 method for signature 'IdtMxSNDE'
var(x)
```

#### **Arguments**

Χ

An object representing a model fitted to interval data.

## Value

For the IdtNDE, IdtSNDE and IdtNandSNDE methods or IdtMxNDE, IdtMxSNDE methods with slot "Hmcdt" equal to TRUE: a matrix with the estimated covariances.

For the IdtMxNDE, and IdtMxSNDE methods with slot "Hmcdt" equal to FALSE: a three-dimensional array with a matrix with the estimated covariances for each group at each level of the third dimension.

#### See Also

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vcov--methods

Methods for function vcov in Package 'MAINT.Data'

#### **Description**

S4 methods for function vcov. As in the generic vcov S3 'stats' method, these methods extract variance-covariance estimates of parameter estimators, for the models fitted to Interval Data.

## Usage

```
## S4 method for signature 'IdtNDE'
vcov(object, selmodel=BestModel(object), ...)
## S4 method for signature 'IdtSNDE'
vcov(object, selmodel=BestModel(object), ...)
## S4 method for signature 'IdtNandSNDE'
vcov(object, selmodel=BestModel(object), ...)
## S4 method for signature 'IdtMxNDE'
vcov(object, selmodel=BestModel(object), group=NULL, ...)
## S4 method for signature 'IdtMxSNDE'
vcov(object, selmodel=BestModel(object), group=NULL, ...)
```

## **Arguments**

object An object representing a model fitted to interval data.

selmodel Selected model from a list of candidate models saved in object.

group The group for each the estimated parameter variance-covariance will be re-

turned. If NULL (default), "vcov" will return a three-dimensional array with a matrix of the estimated covariances between the parameter estimates for each group at each level of the third dimension. Note that this argument is only used in heterocedastic models, i.e. in the IdtMxNDE, IdtMxSNDE methods when the

object slot "Hmcdt" is set to to FALSE.

... Additional arguments for method functions.

#### Value

For the IdtNDE, IdtSNDE and IdtNandSNDE methods or IdtMxNDE, IdtMxSNDE methods with slot "Hmcdt" equal to TRUE: a matrix of the estimated covariances between the parameter estimates. For the IdtMxNDE, and IdtMxSNDE methods with slot "Hmcdt" equal to FALSE: if argument "group" is set to NULL, a three-dimensional array with a matrix of the estimated covariances between the parameter estimates for each group at each level of the third dimension. If argument "group" is set to an integer, the matrix with the estimated covariances between the parameter estimates, for the group chosen.

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# See Also

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