# Package 'ccaPP'

October 12, 2022

Type Package  Title (Robust) Canonical Correlation Analysis via Projection Pursuit  Version 0.3.3  Date 2019-12-09  Depends R (>= 3.2.0), parallel, pcaPP (>= 1.8-1), robustbase  Imports Rcpp (>= 0.11.0)  LinkingTo Rcpp (>= 0.11.0), RcppArmadillo (>= 0.4.100.0)  Suggests knitr, mvtnorm  VignetteBuilder knitr  Description Canonical correlation analysis and maximum correlation via projection pursuit, as well as fast implementations of correlation estimators, with a focus on robust and nonparametric methods.  License GPL (>= 2)  LazyLoad yes  Author Andreas Alfons [aut, cre],    David Simcha [ctb]  Maintainer Andreas Alfons <alfons@ese.eur.nl> Encoding UTF-8  RoxygenNote 6.1.1  NeedsCompilation yes  Repository CRAN  Date/Publication 2019-12-09 12:40:02 UTC  R topics documented:     ccaPP-package    ccaGrid    ccaProj    corFunctions    diabetes</alfons@ese.eur.nl>	
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ccaPP-package ccaGrid ccaProj corFunctions	
ccaGrid	R topics documented:
	ccaGrid

2 ccaPP-package

ccaP	P-package					(F	Roi	bu	st)	) (	Cai	no	ni	ca	l C	Col	rre	ela	ıti	on	A	nc	ıly	sis	s v	ia	Pi	roj	iec	ctio	on	P	ur	su	it			
Index																																						19
	permTest .	•	•	•	•	•		•	•	•	•	•			•	•	•	•		•		•	•	•	•	•	•	•	•	•	•	•		•	•	•	•	17
	maxCorProj																																					
	maxCorGrid																																					13
	fastMedian																																					
	fastMAD .																																					11

# Description

Canonical correlation analysis and maximum correlation via projection pursuit, as well as fast implementations of correlation estimators, with a focus on robust and nonparametric methods.

#### **Details**

## The DESCRIPTION file:

Package: ccaPP Type: Package

Title: (Robust) Canonical Correlation Analysis via Projection Pursuit

Version: 0.3.3

Date: 2019-12-09

Depends: R (>= 3.2.0), parallel, pcaPP (>= 1.8-1), robustbase

Imports: Rcpp ( $\geq 0.11.0$ )

LinkingTo: Rcpp (>= 0.11.0), RcppArmadillo (>= 0.4.100.0)

Suggests: knitr, mvtnorm

VignetteBuilder: knitr

Description: Canonical correlation analysis and maximum correlation via projection pursuit, as well as fast implementa

License: GPL (>= 2)

LazyLoad: yes

Authors@R: c(person("Andreas", "Alfons", email = "alfons@ese.eur.nl", role = c("aut", "cre")), person("David", "Simc

Author: Andreas Alfons [aut, cre], David Simcha [ctb]

Maintainer: Andreas Alfons <alfons@ese.eur.nl>

Encoding: UTF-8 RoxygenNote: 6.1.1

# Index of help topics:

ccaGrid (Robust) CCA via alternating series of grid

searches

ccaPP-package (Robust) Canonical Correlation Analysis via

Projection Pursuit

ccaProj (Robust) CCA via projections through the data

points

ccaGrid 3

corFunctions	Fast implementations of (robust) correlation
	estimators
diabetes	Diabetes data
fastMAD	Fast implementation of the median absolute
	deviation
fastMedian	Fast implementation of the median
maxCorGrid	(Robust) maximum correlation via alternating
	series of grid searches
maxCorProj	(Robust) maximum correlation via projections
	through the data points
permTest	(Robust) permutation test for no association

# Author(s)

Andreas Alfons [aut, cre], David Simcha [ctb]

Maintainer: Andreas Alfons <alfons@ese.eur.nl>

#### References

A. Alfons, C. Croux and P. Filzmoser (2016) Robust maximum association between data sets: The R Package **ccaPP**. *Austrian Journal of Statistics*, **45**(1), 71–79.

A. Alfons, C. Croux and P. Filzmoser (2016) Robust maximum association estimators. *Journal of the American Statistical Association*. DOI 10.1080/01621459.2016.1148609. In press.

ccaGrid

(Robust) CCA via alternating series of grid searches

## Description

Perform canoncial correlation analysis via projection pursuit based on alternating series of grid searches in two-dimensional subspaces of each data set, with a focus on robust and nonparametric methods.

# Usage

```
ccaGrid(x, y, k = 1, method = c("spearman", "kendall", "quadrant", "M",
   "pearson"), control = list(...), nIterations = 10, nAlternate = 10,
   nGrid = 25, select = NULL, tol = 1e-06, standardize = TRUE,
   fallback = FALSE, seed = NULL, ...)
CCAgrid(x, y, k = 1, method = c("spearman", "kendall", "quadrant", "M",
   "pearson"), maxiter = 10, maxalter = 10, splitcircle = 25,
   select = NULL, zero.tol = 1e-06, standardize = TRUE,
   fallback = FALSE, seed = NULL, ...)
```

4 ccaGrid

#### **Arguments**

x, y each can be a numeric vector, matrix or data frame.

k an integer giving the number of canonical variables to compute.

method a character string specifying the correlation functional to maximize. Possible

values are "spearman" for the Spearman correlation, "kendall" for the Kendall correlation, "quadrant" for the quadrant correlation, "M" for the correlation based on a bivariate M-estimator of location and scatter with a Huber loss function, or "pearson" for the classical Pearson correlation (see corFunctions).

control a list of additional arguments to be passed to the specified correlation functional.

If supplied, this takes precedence over additional arguments supplied via the . . .

argument.

nIterations, maxiter

an integer giving the maximum number of iterations.

nAlternate, maxalter

an integer giving the maximum number of alternate series of grid searches in

each iteration.

nGrid, splitcircle

an integer giving the number of equally spaced grid points on the unit circle to

use in each grid search.

select optional; either an integer vector of length two or a list containing two index

vectors. In the first case, the first integer gives the number of variables of x to be randomly selected for determining the order of the variables of y in the corresponding series of grid searches, and vice versa for the second integer. In the latter case, the first list element gives the indices of the variables of x to be used for determining the order of the variables of y, and vice versa for the

second integer (see "Details").

tol, zero.tol a small positive numeric value to be used for determining convergence.

standardize a logical indicating whether the data should be (robustly) standardized.

fallback logical indicating whether a fallback mode for robust standardization should be

used. If a correlation functional other than the Pearson correlation is maximized, the first attempt for standardizing the data is via median and MAD. In the fall-back mode, variables whose MADs are zero (e.g., dummy variables) are standardized via mean and standard deviation. Note that if the Pearson correlation is maximized, standardization is always done via mean and standard deviation.

seed optional initial seed for the random number generator (see .Random. seed). This

is only used if select specifies the numbers of variables of each data set to be randomly selected for determining the order of the variables of the respective

other data set.

... additional arguments to be passed to the specified correlation functional. Cur-

rently, this is only relevant for the M-estimator. For Spearman, Kendall and

quadrant correlation, consistency at the normal model is always forced.

#### **Details**

The algorithm is based on alternating series of grid searches in two-dimensional subspaces of each data set. In each grid search, nGrid grid points on the unit circle in the corresponding plane are

ccaGrid 5

obtained, and the directions from the center to each of the grid points are examined. In the first iteration, equispaced grid points in the interval  $[-\pi/2,\pi/2)$  are used. In each subsequent iteration, the angles are halved such that the interval  $[-\pi/4,\pi/4)$  is used in the second iteration and so on. If only one data set is multivariate, the algorithm simplifies to iterative grid searches in two-dimensional subspaces of the corresponding data set.

In the basic algorithm, the order of the variables in a series of grid searches for each of the data sets is determined by the average absolute correlations with the variables of the respective other data set. Since this requires to compute the full  $(p \times q)$  matrix of absolute correlations, where p denotes the number of variables of x and q the number of variables of y, a faster modification is available as well. In this modification, the average absolute correlations are computed over only a subset of the variables of the respective other data set. It is thereby possible to use randomly selected subsets of variables, or to specify the subsets of variables directly.

Note that also the data sets are ordered according to the maximum average absolute correlation with the respective other data set to ensure symmetry of the algorithm.

For higher order canonical correlations, the data are first transformed into suitable subspaces. Then the alternate grid algorithm is applied to the reduced data and the results are back-transformed to the original space.

## Value

An object of class "cca" with the following components:

cor	a numeric vector giving the canonical correlation measures.
A	a numeric matrix in which the columns contain the canonical vectors for x.
В	a numeric matrix in which the columns contain the canonical vectors for y.
centerX	a numeric vector giving the center estimates used in standardization of x.
centerY	a numeric vector giving the center estimates used in standardization of y.
scaleX	a numeric vector giving the scale estimates used in standardization of x.
scaleY	a numeric vector giving the scale estimates used in standardization of y.
call	the matched function call.

#### Note

CCAgrid is a simple wrapper function for ccaGrid for more compatibility with package **pcaPP** concerning function and argument names.

# Author(s)

Andreas Alfons

#### See Also

ccaProj, maxCorGrid, corFunctions

6 ccaProj

## **Examples**

```
data("diabetes")
x <- diabetes$x
y <- diabetes$y
## Spearman correlation
ccaGrid(x, y, method = "spearman")
## Pearson correlation
ccaGrid(x, y, method = "pearson")
```

ccaProj

(Robust) CCA via projections through the data points

# **Description**

Perform canoncial correlation analysis via projection pursuit based on projections through the data points, with a focus on robust and nonparametric methods.

#### Usage

```
ccaProj(x, y, k = 1, method = c("spearman", "kendall", "quadrant", "M",
  "pearson"), control = list(...), standardize = TRUE,
  useL1Median = TRUE, fallback = FALSE, ...)
CCAproj(x, y, k = 1, method = c("spearman", "kendall", "quadrant", "M",
  "pearson"), standardize = TRUE, useL1Median = TRUE,
  fallback = FALSE, ...)
```

## **Arguments**

each can be a numeric vector, matrix or data frame. х, у

k an integer giving the number of canonical variables to compute.

method a character string specifying the correlation functional to maximize. Possible

> values are "spearman" for the Spearman correlation, "kendall" for the Kendall correlation, "quadrant" for the quadrant correlation, "M" for the correlation based on a bivariate M-estimator of location and scatter with a Huber loss func-

tion, or "pearson" for the classical Pearson correlation (see corFunctions).

control a list of additional arguments to be passed to the specified correlation functional.

If supplied, this takes precedence over additional arguments supplied via the . . .

argument.

standardize a logical indicating whether the data should be (robustly) standardized.

useL1Median a logical indicating whether the  $L_1$  medians should be used as the centers of the

> data sets in standardization (defaults to TRUE). If FALSE, the columnwise centers are used instead (columnwise means if method is "pearson" and columnwise

medians otherwise).

ccaProj 7

fallback logical indicating whether a fallback mode for robust standardization should be

used. If a correlation functional other than the Pearson correlation is maximized, the first attempt for standardizing the data is via median and MAD. In the fall-back mode, variables whose MADs are zero (e.g., dummy variables) are standardized via mean and standard deviation. Note that if the Pearson correlation is maximized, standardization is always done via mean and standard deviation.

. . additional arguments to be passed to the specified correlation functional. Cur-

rently, this is only relevant for the M-estimator. For Spearman, Kendall and

quadrant correlation, consistency at the normal model is always forced.

## **Details**

First the candidate projection directions are defined for each data set from the respective center through each data point. Then the algorithm scans all  $n^2$  possible combinations for the maximum correlation, where n is the number of observations.

For higher order canonical correlations, the data are first transformed into suitable subspaces. Then the alternate grid algorithm is applied to the reduced data and the results are back-transformed to the original space.

#### Value

An object of class "cca" with the following components:

cor a numeric vector giving the canonical correlation measures.

a numeric matrix in which the columns contain the canonical vectors for x.

B a numeric matrix in which the columns contain the canonical vectors for y.

centerX a numeric vector giving the center estimates used in standardization of x.

centerY a numeric vector giving the center estimates used in standardization of y.

scaleX a numeric vector giving the scale estimates used in standardization of x.

scaleY a numeric vector giving the scale estimates used in standardization of y.

the matched function call.

#### Note

CCAproj is a simple wrapper function for ccaProj for more compatibility with package **pcaPP** concerning function names.

#### Author(s)

Andreas Alfons

#### See Also

ccaGrid, maxCorProj, corFunctions

8 corFunctions

# **Examples**

```
data("diabetes")
x <- diabetes$x
y <- diabetes$y

## Spearman correlation
ccaProj(x, y, method = "spearman")

## Pearson correlation
ccaProj(x, y, method = "pearson")</pre>
```

corFunctions

Fast implementations of (robust) correlation estimators

# **Description**

Estimate the correlation of two vectors via fast C++ implementations, with a focus on robust and nonparametric methods.

# Usage

```
corPearson(x, y)
corSpearman(x, y, consistent = FALSE)

corKendall(x, y, consistent = FALSE)

corQuadrant(x, y, consistent = FALSE)

corM(x, y, prob = 0.9, initial = c("quadrant", "spearman", "kendall", "pearson"), tol = 1e-06)
```

## **Arguments**

x, y	numeric vectors.
consistent	a logical indicating whether a consistent estimate at the bivariate normal distribution should be returned (defaults to FALSE).
prob	numeric; probability for the quantile of the $\chi^2$ distribution to be used for tuning the Huber loss function (defaults to 0.9).
initial	a character string specifying the starting values for the Huber M-estimator. For "quadrant" (the default), "spearman" or "kendall", the consistent version of the respecive correlation measure is used together with the medians and MAD's. For "pearson", the Pearson correlation is used together with the means and standard deviations.
tol	a small positive numeric value to be used for determining convergence.

corFunctions 9

#### **Details**

corPearson estimates the classical Pearson correlation. corSpearman, corKendall and corQuadrant estimate the Spearman, Kendall and quadrant correlation, respectively, which are nonparametric correlation measures that are somewhat more robust. corM estimates the correlation based on a bivariate M-estimator of location and scatter with a Huber loss function, which is sufficiently robust in the bivariate case, but loses robustness with increasing dimension.

The nonparametric correlation measures do not estimate the same population quantities as the Pearson correlation, the latter of which is consistent at the bivariate normal model. Let  $\rho$  denote the population correlation at the normal model. Then the Spearman correlation estimates  $(6/\pi) \arcsin(\rho/2)$ , while the Kendall and quadrant correlation estimate  $(2/\pi) \arcsin(\rho)$ . Consistent estimates are thus easily obtained by taking the corresponding inverse expressions.

The Huber M-estimator, on the other hand, is consistent at the bivariate normal model.

#### Value

The respective correlation estimate.

#### Note

The Kendall correlation uses a naive  $n^2$  implementation if n < 30 and a fast  $O(n \log(n))$  implementation for larger values, where n denotes the number of observations.

Functionality for removing observations with missing values is currently not implemented.

# Author(s)

Andreas Alfons,  $O(n \log(n))$  implementation of the Kendall correlation by David Simcha

#### See Also

```
ccaGrid, ccaProj, cor
```

# **Examples**

```
## generate data
library("mvtnorm")
set.seed(1234) # for reproducibility
sigma <- matrix(c(1, 0.6, 0.6, 1), 2, 2)
xy <- rmvnorm(100, sigma=sigma)
x <- xy[, 1]
y <- xy[, 2]

## compute correlations

# Pearson correlation
corPearson(x, y)

# Spearman correlation
corSpearman(x, y)
corSpearman(x, y, consistent=TRUE)</pre>
```

10 diabetes

```
# Kendall correlation
corKendall(x, y)
corKendall(x, y, consistent=TRUE)
# quadrant correlation
corQuadrant(x, y)
corQuadrant(x, y, consistent=TRUE)
# Huber M-estimator
corM(x, y)
```

diabetes

Diabetes data

# **Description**

Subset of the diabetes data from Andrews & Herzberg (1985).

## Usage

data(diabetes)

## **Format**

A list with components x and y. Both components are matrices with observations on different variables for the same n=76 persons.

Component x is a matrix containing the following p = 2 variables.

RelativeWeight relative weight.

PlasmaGlucose fasting plasma glucose.

Component y is a matrix containing the following q=3 variables.

GlucoseIntolerance glucose intolerance.

InsulinResponse insulin response to oral glucose.

InsulinResistance insulin resistance.

#### **Source**

Andrews, D.F. and Herzberg, A.M. (1985) Data. Springer-Verlag. Page 215.

fastMAD 11

## **Examples**

```
data("diabetes")
x <- diabetes$x
y <- diabetes$y

## Spearman correlation
maxCorGrid(x, y, method = "spearman")
maxCorGrid(x, y, method = "spearman", consistent = TRUE)

## Pearson correlation
maxCorGrid(x, y, method = "pearson")</pre>
```

fastMAD

Fast implementation of the median absolute deviation

## **Description**

Compute the median absolute deviation with a fast C++ implementation. By default, a multiplication factor is applied for consistency at the normal model.

# Usage

```
fastMAD(x, constant = 1.4826)
```

# Arguments

x a numeric vector.

constant a numeric multiplication factor. The default value yields consistency at the nor-

mal model.

#### Value

A list with the following components:

center a numeric value giving the sample median.

MAD a numeric value giving the median absolute deviation.

#### Note

Functionality for removing observations with missing values is currently not implemented.

## Author(s)

Andreas Alfons

## See Also

fastMedian, mad

12 fastMedian

# **Examples**

```
set.seed(1234) # for reproducibility
x <- rnorm(100)
fastMAD(x)</pre>
```

fastMedian

Fast implementation of the median

# Description

Compute the sample median with a fast C++ implementation.

# Usage

```
fastMedian(x)
```

# Arguments

Х

a numeric vector.

# Value

The sample median.

# Note

Functionality for removing observations with missing values is currently not implemented.

# Author(s)

Andreas Alfons

## See Also

```
fastMAD, median
```

# **Examples**

```
set.seed(1234) # for reproducibility
x <- rnorm(100)
fastMedian(x)</pre>
```

maxCorGrid 13

maxCorGrid	(Robust) maximum correlation via alternating series of grid searches

# Description

Compute the maximum correlation between two data sets via projection pursuit based on alternating series of grid searches in two-dimensional subspaces of each data set, with a focus on robust and nonparametric methods.

# Usage

```
maxCorGrid(x, y, method = c("spearman", "kendall", "quadrant", "M",
   "pearson"), control = list(...), nIterations = 10, nAlternate = 10,
   nGrid = 25, select = NULL, tol = 1e-06, standardize = TRUE,
   fallback = FALSE, seed = NULL, ...)
```

# **Arguments**

fallback

Ę	guments	
	x, y	each can be a numeric vector, matrix or data frame.
	method	a character string specifying the correlation functional to maximize. Possible values are "spearman" for the Spearman correlation, "kendall" for the Kendall correlation, "quadrant" for the quadrant correlation, "M" for the correlation based on a bivariate M-estimator of location and scatter with a Huber loss function, or "pearson" for the classical Pearson correlation (see corFunctions).
	control	a list of additional arguments to be passed to the specified correlation functional. If supplied, this takes precedence over additional arguments supplied via the $\dots$ argument.
	nIterations	an integer giving the maximum number of iterations.
	nAlternate	an integer giving the maximum number of alternate series of grid searches in each iteration.
	nGrid	an integer giving the number of equally spaced grid points on the unit circle to use in each grid search.
	select	optional; either an integer vector of length two or a list containing two index vectors. In the first case, the first integer gives the number of variables of x to be randomly selected for determining the order of the variables of y in the corresponding series of grid searches, and vice versa for the second integer. In the latter case, the first list element gives the indices of the variables of x to be used for determining the order of the variables of y, and vice versa for the second integer (see "Details").
	tol	a small positive numeric value to be used for determining convergence.
	standardize	a logical indicating whether the data should be (robustly) standardized.

logical indicating whether a fallback mode for robust standardization should be used. If a correlation functional other than the Pearson correlation is maximized,

14 maxCorGrid

the first attempt for standardizing the data is via median and MAD. In the fall-back mode, variables whose MADs are zero (e.g., dummy variables) are standardized via mean and standard deviation. Note that if the Pearson correlation is maximized, standardization is always done via mean and standard deviation.

seed optional initial seed for the random number generator (see .Random.seed). This

is only used if select specifies the numbers of variables of each data set to be randomly selected for determining the order of the variables of the respective

other data set.

... additional arguments to be passed to the specified correlation functional.

#### **Details**

The algorithm is based on alternating series of grid searches in two-dimensional subspaces of each data set. In each grid search, nGrid grid points on the unit circle in the corresponding plane are obtained, and the directions from the center to each of the grid points are examined. In the first iteration, equispaced grid points in the interval  $[-\pi/2,\pi/2)$  are used. In each subsequent iteration, the angles are halved such that the interval  $[-\pi/4,\pi/4)$  is used in the second iteration and so on. If only one data set is multivariate, the algorithm simplifies to iterative grid searches in two-dimensional subspaces of the corresponding data set.

In the basic algorithm, the order of the variables in a series of grid searches for each of the data sets is determined by the average absolute correlations with the variables of the respective other data set. Since this requires to compute the full  $(p \times q)$  matrix of absolute correlations, where p denotes the number of variables of x and q the number of variables of y, a faster modification is available as well. In this modification, the average absolute correlations are computed over only a subset of the variables of the respective other data set. It is thereby possible to use randomly selected subsets of variables, or to specify the subsets of variables directly.

Note that also the data sets are ordered according to the maximum average absolute correlation with the respective other data set to ensure symmetry of the algorithm.

#### Value

An object of class "maxCor" with the following components:

cor a numeric giving the maximum correlation estimate.

a numeric; the weighting vector for x.b numeric; the weighting vector for y.

centerX a numeric vector giving the center estimates used in standardization of x.

centerY a numeric vector giving the center estimates used in standardization of y.

scaleX a numeric vector giving the scale estimates used in standardization of x.

scaleY a numeric vector giving the scale estimates used in standardization of y.

call the matched function call.

## Author(s)

Andreas Alfons

maxCorProj 15

## References

A. Alfons, C. Croux and P. Filzmoser (2016) Robust maximum association between data sets: The R Package **ccaPP**. *Austrian Journal of Statistics*, **45**(1), 71–79.

A. Alfons, C. Croux and P. Filzmoser (2016) Robust maximum association estimators. *Journal of the American Statistical Association*. DOI 10.1080/01621459.2016.1148609. In press.

#### See Also

```
maxCorProj, ccaGrid, corFunctions
```

## **Examples**

```
data("diabetes")
x <- diabetes$x
y <- diabetes$y

## Spearman correlation
maxCorGrid(x, y, method = "spearman")
maxCorGrid(x, y, method = "spearman", consistent = TRUE)

## Pearson correlation
maxCorGrid(x, y, method = "pearson")</pre>
```

maxCorProj

(Robust) maximum correlation via projections through the data points

## **Description**

Compute the maximum correlation between two data sets via projection pursuit based on projections through the data points, with a focus on robust and nonparametric methods.

## Usage

```
maxCorProj(x, y, method = c("spearman", "kendall", "quadrant", "M",
    "pearson"), control = list(...), standardize = TRUE,
    useL1Median = TRUE, fallback = FALSE, ...)
```

## **Arguments**

х, у

each can be a numeric vector, matrix or data frame.

method

a character string specifying the correlation functional to maximize. Possible values are "spearman" for the Spearman correlation, "kendall" for the Kendall correlation, "quadrant" for the quadrant correlation, "M" for the correlation based on a bivariate M-estimator of location and scatter with a Huber loss function, or "pearson" for the classical Pearson correlation (see corFunctions).

16 maxCorProj

control a list of additional arguments to be passed to the specified correlation functional.

If supplied, this takes precedence over additional arguments supplied via the . . .

argument.

standardize a logical indicating whether the data should be (robustly) standardized.

useL1Median a logical indicating whether the  $L_1$  medians should be used as the centers of the

data sets in standardization (defaults to TRUE). If FALSE, the columnwise centers are used instead (columnwise means if method is "pearson" and columnwise

medians otherwise).

fallback logical indicating whether a fallback mode for robust standardization should be

used. If a correlation functional other than the Pearson correlation is maximized, the first attempt for standardizing the data is via median and MAD. In the fall-back mode, variables whose MADs are zero (e.g., dummy variables) are standardized via mean and standard deviation. Note that if the Pearson correlation is maximized, standardization is always done via mean and standard deviation.

... additional arguments to be passed to the specified correlation functional.

#### **Details**

First the candidate projection directions are defined for each data set from the respective center through each data point. Then the algorithm scans all  $n^2$  possible combinations for the maximum correlation, where n is the number of observations.

#### Value

An object of class "maxCor" with the following components:

cor a numeric giving the maximum correlation estimate.

a numeric; the weighting vector for x.b numeric; the weighting vector for y.

centerX a numeric vector giving the center estimates used in standardization of x.

centerY a numeric vector giving the center estimates used in standardization of y.

scaleX a numeric vector giving the scale estimates used in standardization of x.

scaleY a numeric vector giving the scale estimates used in standardization of y.

call the matched function call.

#### Author(s)

Andreas Alfons

#### See Also

maxCorGrid, ccaProj, corFunctions,

permTest 17

## **Examples**

```
data("diabetes")
x <- diabetes$x
y <- diabetes$y

## Spearman correlation
maxCorProj(x, y, method = "spearman")
maxCorProj(x, y, method = "spearman", consistent = TRUE)

## Pearson correlation
maxCorProj(x, y, method = "pearson")</pre>
```

permTest

(Robust) permutation test for no association

## **Description**

Test whether or not there is association betwenn two data sets, with a focus on robust and nonparametric correlation measures.

## Usage

```
permTest(x, y, R = 1000, fun = maxCorGrid, permutations = NULL,
   nCores = 1, cl = NULL, seed = NULL, ...)
```

## Arguments

x, y each can be a numeric vector, matrix or data frame.

R an integer giving the number of random permutations to be used.

fun a function to compute a maximum correlation measure between two data sets,

e.g., maxCorGrid (the default) or maxCorProj. It should expect the data to be passed as the first and second argument, and must return an object of class

"maxCor".

permutations an integer matrix in which each column contains the indices of a permutation.

If supplied, this is preferred over R.

nCores a positive integer giving the number of processor cores to be used for parallel

computing (the default is 1 for no parallelization). If this is set to NA, all available

processor cores are used.

cl a **parallel** cluster for parallel computing as generated by makeCluster. If sup-

plied, this is preferred over nCores.

seed optional integer giving the initial seed for the random number generator (see

. Random. seed). For parallel computing, random number streams are used rather

than the standard random number generator and the seed is set via clusterSetRNGStream.

. . . additional arguments to be passed to fun.

18 permTest

#### **Details**

The test generates R data sets by randomly permuting the observations of x, while keeping the observations of y fixed. In each replication, a function to compute a maximum correlation measure is applied to the permuted data sets. The p-value of the test is then given by the percentage of replicates of the maximum correlation measure that are larger than the maximum correlation measure computed from the original data.

## Value

An object of class "permTest" with the following components:

pValue the p-value for the test. cor0 the value of the test statistic.

cor the values of the test statistic for each of the permutated data sets.

R the number of random permutations.

seed the seed of the random number generator.

call the matched function call.

## Author(s)

Andreas Alfons

#### References

A. Alfons, C. Croux and P. Filzmoser (2016) Robust maximum association between data sets: The R Package **ccaPP**. *Austrian Journal of Statistics*, **45**(1), 71–79.

#### See Also

```
maxCorGrid, maxCorProj
```

# **Examples**

```
data("diabetes")
x <- diabetes$x
y <- diabetes$y

## Spearman correlation
permTest(x, y, R = 100, method = "spearman")
permTest(x, y, R = 100, method = "spearman", consistent = TRUE)

## Pearson correlation
permTest(x, y, R = 100, method = "pearson")</pre>
```

# **Index**

* datasets	fastMAD, 11, <i>12</i>
diabetes, 10	fastMedian, <i>11</i> , 12
* multivariate	
ccaGrid, 3	mad, <i>11</i>
ccaProj,6	makeCluster, 17
corFunctions, 8	maxCorGrid, 5, 13, 16–18
fastMAD, 11	maxCorProj, 7, 15, 15, 17, 18
fastMedian, 12	median, 12
maxCorGrid, 13	T+ 17
maxCorProj, 15	permTest, 17
permTest, 17	print.cca (ccaGrid), 3
* package	<pre>print.maxCor (maxCorGrid), 13</pre>
ccaPP-package, 2	
* robust	
ccaGrid, 3	
ccaProj,6	
corFunctions, $8$	
fastMAD, 11	
fastMedian, 12	
maxCorGrid, 13	
maxCorProj, 15	
permTest, 17	
.Random.seed, 4, 14, 17	
CCAgrid (ccaGrid), 3	
ccaGrid, 3, 7, 9, 15	
ccaPP (ccaPP-package), 2	
ccaPP-package, 2	
CCAproj (ccaProj), 6	
ccaProj, 5, 6, 9, 16	
clusterSetRNGStream, 17	
cor, 9	
corFunctions, <i>4</i> –7, 8, <i>13</i> , <i>15</i> , <i>16</i>	
corKendall (corFunctions), 8	
corM (corFunctions), 8	
corPearson ( $corFunctions$ ), $8$	
$\operatorname{corQuadrant}(\operatorname{corFunctions}), 8$	
corSpearman (corFunctions), 8	
diabetes, 10	