

# Package ‘MCCM’

January 20, 2025

**Title** Mixed Correlation Coefficient Matrix

**Version** 0.1.0

**Description** The IRLS (Iteratively Reweighted Least Squares) and GMM (Generalized Method of Moments) methods are applied to estimate mixed correlation coefficient matrix (Pearson, Polychoric, Polyserial), which can be estimated in pairs or simultaneously. For more information see Peng Zhang and Ben Liu (2024) <[doi:10.1080/10618600.2023.2257251](https://doi.org/10.1080/10618600.2023.2257251)>; Ben Liu and Peng Zhang (2024) <[doi:10.1080/10618600.2023.2257251](https://doi.org/10.1080/10618600.2023.2257251)>

**License** GPL

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**NeedsCompilation** no

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CECERS	<i>Chinese Early Childhood Environment Rating Scale</i>
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### Description

The CECERS uses a 9-point scoring system, 1-3 (inadequate), 5 (least acceptable), 7 (good), and 9 (excellent), to measure the quality of Chinese early children education (ECE) programs for children aged 3 to 6. The CECERS has a total of 51 items organized in eight categories: (1) Space and Furnishings (9 items); (2) Personal Care Routines (6 items); (3) Curriculum Planning and Implementation (5 items); (4) Whole-Group Instruction (7 items); (5) Activities (9 items); (6) Language-Reasoning (4 items); (7) Guidance and Interaction (5 items); (8) Parents and Staff (6 items).

### Format

A data frame with 1383 rows and 95 variables:

### Source

Kejian Li, Peng Zhang, Bi Ying Hu, Margaret R Burchinal, Xitao Fan, and Jinliang Qin. Testing the ‘thresholds’ of preschool education quality on child outcomes in china. *Early Childhood Research Quarterly*, 47:445–456, 2019.

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dphixy	<i>Scaled Bivariate Normal Density</i>
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---

### Description

Bivariate normal density with mean 0 variance 1.

### Usage

dphixy(x, y, rho)

**Arguments**

x, y            points value.  
rho            correlation coefficient.

**Value**

the density value.

**Examples**

```
library(mvtnorm)
dmvnorm(c(1,-1),sigma = matrix(c(1,0.5,0.5,1),2,2))
dphixy(1,-1,0.5)
```

---

draw\_correlation\_matrix

*Draw the Correlation Matrix*

---

**Description**

Estimate the MCCM from dataframe and draw it with scatter plot of matrices (SPLOM). With bivariate scatter plots below the diagonal, histograms on the diagonal, and the polychoric correlation coefficients with standard errors above the diagonal. Correlation ellipses are drawn in the same graph. The red lines below the diagonal are the LOESS smoothed lines, fitting a smooth curve between two variables.

**Usage**

```
draw_correlation_matrix(  
  data1,  
  order_indx,  
  pair_est = FALSE,  
  MLE = FALSE,  
  R0 = NULL,  
  app = TRUE,  
  korder = 2,  
  max_iter = 1000,  
  max_tol = 1e-08,  
  show_log = FALSE  
)
```

**Arguments**

data1            a dataframe containing continuous or ordinal variable.  
order\_indx        a vector to indicate the ordinal variables.  
pair\_est          bool value, TRUE for pairwise estimation, FALSE for simultaneous estimation.

MLE	bool value, TRUE for maximum likelihood estimation, FALSE for IRLS (pairwise) or IGMM (simultaneous) estimation.
R0	the initial value for correlation vector, default Pearson correlation matrix.
app	bool value for approximation, TRUE for Legendre approximation, FALSE for common integral.
korder	the order of Legendre approximation.
max_iter	max iteration number for IGMM.
max_tol	max tolerance for iteration algorithm.
show_log	bool value, TRUE for showing calculation log.

**Value**

the SPLOM plot.

**See Also**

[MCCM\\_est](#), [summary\\_MCCM\\_est](#)

**Examples**

```

library(mvtnorm)
library(MASS)
library(polycor)
library(lavaan)
set.seed(1997)
n = 10000
rho12=0.3
rho13=0.4
rho14=0.5
rho23=0.6
rho24=0.7
rho34=0.8

R = matrix(c(1,rho12,rho13,rho14,rho12,1,rho23,rho24,rho13,rho23,1,rho34,
rho14,rho24,rho34,1),4,4)
indc = c(3,4)
thresholds = list(c(),c(),0,0)
data1 = gen_mixed(n=n,R=R,indc=indc,thresholds=thresholds)
data2 = data.frame(data1$observed)

# pairwise MLE estimation
draw_correlation_matrix(data2,indc,TRUE,TRUE)
# pairwise IRLS estimation
draw_correlation_matrix(data2,indc,TRUE,FALSE)
# simultaneous MLE estimation
draw_correlation_matrix(data2,indc,FALSE,TRUE)
# simultaneous IGMM estimation
draw_correlation_matrix(data2,indc,FALSE,FALSE)

```

---

esti_polychoric	<i>Polychoric Correlation</i>
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---

**Description**

Estimate the polychoric correlation coefficient.

**Usage**

```
esti_polychoric(X, maxn = 100, e = 1e-08, ct = FALSE)
```

**Arguments**

X	a matrix(2*N) or dataframe contains two polychoric variable, or a contingency table with both columns and rows names.
maxn	the maximum iterations times.
e	the maximum tolerance of convergence.
ct	TRUE for contingency table, FALSE for matrix or dataframe

**Value**

rho	estimated value of polychoric correlation coefficient.
std	standard deviation of rho.
iter	times of iteration convergence.
Ex, Ey	the support points series of regression model

**References**

Zhang, P., Liu, B., & Pan, J. (2024). Iteratively Reweighted Least Squares Method for Estimating Polyserial and Polychoric Correlation Coefficients. *Journal of Computational and Graphical Statistics*, 33(1), 316–328. <https://doi.org/10.1080/10618600.2023.2257251>

**See Also**

[esti\\_polyserial](#)

**Examples**

```
X = gen_polychoric(1000,0.5,0:1,-1:0)
result = esti_polychoric(X)
print(c(result$rho,result$std,result$iter))
```

---

esti\_polyserial      *Polyserial Correlation*

---

### Description

Estimate the polyserial correlation coefficient.

### Usage

```
esti_polyserial(X, maxn = 100, e = 1e-08)
```

### Arguments

X	a matrix(2*N) or dataframe contains two polyserial variable(Continuous variable first).
maxn	the maximum iterations times.
e	the maximum tolerance of convergence.

### Value

rho	estimated value of polyserial correlation coefficient.
std	standard deviation of rho.
iter	times of iteration convergence.
Ex, Ey	the support point of regression model.

### References

Zhang, P., Liu, B., & Pan, J. (2024). Iteratively Reweighted Least Squares Method for Estimating Polyserial and Polychoric Correlation Coefficients. *Journal of Computational and Graphical Statistics*, 33(1), 316–328. <https://doi.org/10.1080/10618600.2023.2257251>

### See Also

[esti\\_polychoric](#)

### Examples

```
X = gen_polyseries(1000,0.5,-1:1)
result = esti_polyserial(X)
result
```

---

`est_mixedGMM`*Estimating Mixed Correlation Matrix by IGMM*

---

## Description

An accelerated function to estimate a mixed correlation coefficient matrix, as well as its covariance matrix, for dataframes containing continuous and ordinal variable.

## Usage

```
est_mixedGMM(  
  dataYX,  
  order_indx,  
  R0 = NULL,  
  app = TRUE,  
  korder = 2,  
  max_iter = 1000,  
  max_tol = 1e-08,  
  show_log = FALSE  
)
```

## Arguments

<code>dataYX</code>	a dataframe or matrix containing both continuous and ordinal variables.
<code>order_indx</code>	a vector to indicate the ordinal variables.
<code>R0</code>	the initial value for correlation vector, default Pearson correlation matrix.
<code>app</code>	bool value for approximation, TRUE for Legendre approximation, FALSE for common integral.
<code>korder</code>	the order of Legendre approximation.
<code>max_iter</code>	max iteration number for IGMM.
<code>max_tol</code>	max tolerance for iteration algorithm.
<code>show_log</code>	bool value, TRUE for showing calculation log.

## Value

<code>Rhat</code>	The estimated correlation coefficients.
<code>COV</code>	The estimated covariance matrix for Rhat

## References

arXiv:2404.06781

**Examples**

```

library(mvtnorm)
library(MASS)
set.seed(1997)
n = 500
rho12=0.3
rho13=0.4
rho14=0.5
rho23=0.6
rho24=0.7
rho34=0.8

R = matrix(c(1,rho12,rho13,rho14,rho12,1,rho23,rho24,rho13,rho23,1,rho34,
rho14,rho24,rho34,1),4,4)
indc = c(3,4)
thresholds = list(c(),c(),0,0)
data1 = gen_mixed(n=n,R=R,indc=indc,thresholds=thresholds)
data2 = data.frame(data1$observed)
out1 = est_mixedGMM(dataYX = data2,order_indx = indc)
print(out1$Rhat)
print(out1$COV)

```

---

est\_thre

*Thresholds Estimation*


---

**Description**

Function to calculate thresholds from ordinal variables.

**Usage**

```
est_thre(X)
```

**Arguments**

X                    a ordinal series.

**Value**

the estimated value for thresholds.

**Examples**

```

library(mvtnorm)
set.seed(1997)
R1 = gen_CCM(4)
n = 1000
indc = 3:4
thresholds = list(c(),c(),c(-1),c(1))

```



```
data1 = gen_mixed(n,R1,indc,thresholds=thresholds)$observed
est_thre(data1[,3])
est_thre(data1[,4])
```

---

gen\_CCM

*Positive Semidefinite Correlation Matrix*

---

### Description

Generate a positive semidefinite correlation coefficients matrix

### Usage

```
gen_CCM(d)
```

### Arguments

d                    the dimension of matrix.

### Value

a correlation coefficients matrix.

### Examples

```
X = gen_CCM(4)
print(X)
```

---

gen\_mixed

*Continuous and Ordinal Simulated Data*

---

### Description

Generate multi-normal sample and segment it into ordinal.

### Usage

```
gen_mixed(n, R, indc, thresholds)
```

### Arguments

n                    the sample size.  
R                    the correlation coefficient matrix.  
indc                vector to indicate whether variables are continuous or categorical.  
thresholds        list contains thresholds for ordinal variables

**Value**

latent	the original normal data.
observed	the observed ordinal data.

**Examples**

```
library(mvtnorm)
set.seed(1997)
R1 = gen_CCM(6)
n = 1000
indc = 4:6
thresholds = list(
  c(),
  c(),
  c(),
  c(0),
  c(-0.5,0),
  c(0,0.5)
)
data1 = gen_mixed(n,R1,indc,thresholds)$observed
data1 = data.frame(data1)
table(data1$X4,data1$X5)
table(data1$X5,data1$X6)
```

---

gen_polychoric	<i>Generate Polychoric Sample</i>
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---

**Description**

Generate polychoric sample with hidden distribution: binormal with correlation coefficient rho.

**Usage**

```
gen_polychoric(n, rho, a, b)
```

**Arguments**

n	sample size.
rho	correlation coefficient.
a	the cutoff points array.
b	the cutoff points array.

**Value**

Polychoric sample with size n(in a 2\*n matrix).

**See Also**

[gen\\_polyseries](#) [gen\\_rho](#)

**Examples**

```
gen_polychoric(100,0.5,-1:1,1:2)
```

---

gen_polyseries	<i>Generate Polyseries Sample</i>
----------------	-----------------------------------

---

**Description**

Generate polyseries sample with hidden distribution: binormal with correlation coefficient rho.

**Usage**

```
gen_polyseries(n, rho, a)
```

**Arguments**

n	sample size.
rho	correlation coefficient.
a	the cutoff points array.

**Value**

Polyseries sample with size n(in a 2\*n matrix).

**See Also**

[gen\\_rho](#) [gen\\_polychoric](#)

**Examples**

```
gen_polyseries(100,0.5,-1:1)
```

---

gen_rho	<i>Generate Specific Binormal Distribution</i>
---------	--

---

**Description**

Generate random number of binormal distribution with 0 mean unit variance and correlation coefficient rho.

**Usage**

```
gen_rho(n, rho)
```

**Arguments**

n	sample size.
rho	correlation coefficient.

**Value**

Binormal random number with length n(in a 2\*n matrix).

**See Also**

[gen\\_polyseries](#) [gen\\_polychoric](#)

**Examples**

```
gen_rho(100,0.5)
```

---

mb	<i>Mean Bias</i>
----	------------------

---

**Description**

Calculate the MB of an array of estimates relative to the true value.

**Usage**

```
mb(rhohat, rho)
```

**Arguments**

rhohat	an array of estimators of rho.
rho	the true value of rho.

**Value**

the mean bias of rho-hat array.

**See Also**

[mrb rmse](#)

**Examples**

```
rho = 0.5
rho-hat = 0.5 + rnorm(10)
mb(rho-hat, rho)
```

---

MCCM\_est

*General Function to Estimate Mixed Correlation Coefficient Matrix*


---

**Description**

Estimate the correlation matrix for dataframes containing continuous and ordinal variable, in pairs or simultaneously, using MLE, IRLS, or IGMM.

**Usage**

```
MCCM_est(
  dataYX,
  order_indx,
  pair_est = FALSE,
  MLE = FALSE,
  R0 = NULL,
  app = TRUE,
  korder = 2,
  max_iter = 1000,
  max_tol = 1e-08,
  show_log = FALSE
)
```

**Arguments**

dataYX	a dataframe or matrix containing both continuous and ordinal variables.
order_indx	a vector to indicate the ordinal variables.
pair_est	bool value, TRUE for pairwise estimation, FALSE for simultaneous estimation.
MLE	bool value, TRUE for maximum likelihood estimation, FALSE for IRLS (pair-wise) or IGMM (simultaneous) estimation.
R0	the initial value for correlation vector, default Pearson correlation matrix.
app	bool value for approximation, TRUE for Legendre approximation, FALSE for common integral.

korder	the order of Legendre approximation.
max_iter	max iteration number for IGMM.
max_tol	max tolerance for iteration algorithm.
show_log	bool value, TRUE for showing calculation log.

**Value**

Rmatrix	Estimated mixed correlation coefficient matrix.
std_matrix	Estimated standard deviation for each mixed correlation coefficient.
COV	The covariance matrix for MCCM (simultaneous estimation only).

**See Also**

[esti\\_polyserial](#), [esti\\_polychoric](#), [est\\_mixedGMM](#), [summary\\_MCCM\\_est](#), [draw\\_correlation\\_matrix](#)

**Examples**

```
library(mvtnorm)
library(MASS)
library(polycor)
library(lavaan)
set.seed(1997)
n = 10000
rho12=0.3
rho13=0.4
rho14=0.5
rho23=0.6
rho24=0.7
rho34=0.8

R = matrix(c(1,rho12,rho13,rho14,rho12,1,rho23,rho24,rho13,rho23,1,rho34,
rho14,rho24,rho34,1),4,4)
indc = c(3,4)
thresholds = list(c(),c(),0,0)
data1 = gen_mixed(n=n,R=R,indc=indc,thresholds=thresholds)
data2 = data.frame(data1$observed)

# pairwise MLE estimation
out_pair_MLE = MCCM_est(dataYX=data2,order_indx=indc,pair_est=TRUE,MLE=TRUE)
# pairwise IRLS estimation
out_pair_IRLS = MCCM_est(dataYX=data2,order_indx=indc,pair_est=TRUE,MLE=FALSE)
# simultaneous MLE estimation
out_sim_MLE = MCCM_est(dataYX=data2,order_indx=indc,pair_est=FALSE,MLE=TRUE)
# simultaneous IGMM estimation
out_sim_IGMM = MCCM_est(dataYX=data2,order_indx=indc,pair_est=FALSE,MLE=FALSE)

summary_MCCM_est(out_pair_MLE)
summary_MCCM_est(out_pair_IRLS)
summary_MCCM_est(out_sim_MLE)
summary_MCCM_est(out_sim_IGMM)
```

---

mrb	<i>Mean Relative Bias</i>
-----	---------------------------

---

**Description**

Calculate the MRB of an array of estimates relative to the true value.

**Usage**

```
mrb(rhohat, rho)
```

**Arguments**

rhohat	an array of estimators of rho.
rho	the true value of rho.

**Value**

the mean relative bias of rhohat array.

**See Also**

[mb](#) [rmse](#)

**Examples**

```
rho = 0.5
rhohat = 0.5 + rnorm(10)
mrb(rhohat, rho)
```

---

Parenteral_nutrition	<i>Parenteral_nutrition</i>
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---

**Description**

The Parenteral Nutrition data were collected from 543 patients of whom 386 were given parenteral nutrition alone, 145 were given enteral and parenteral nutrition, and 3 were given enteral nutrition only. There are 23 main discrete variables, such as: clinical stages(1-4), dietary status(1-3), NRS(0-6), PG-SGA-qualitative(1-3), etc.

**Format**

A data frame with 1086 rows and 29 variables:

---

 Phixy

*Scaled Bivariate Normal Approximation*


---

**Description**

Standard bivariate normal distribution approximated with Legendre polynomials.

**Usage**

```
Phixy(x, y, rho, korder = 3, app = TRUE)
```

**Arguments**

x, y	P( $X \leq x, Y \leq y$ ).
rho	correlation coefficient.
korder	order of Legendre approximation.
app	bool value TRUE for approximation, FALSE for integral.

**Value**

P( $X \leq x, Y \leq y$ ).

**Examples**

```
library(mvtnorm)
pmvnorm(upper = c(1,-1),sigma = matrix(c(1,0.5,0.5,1),2,2))
Phixy(1,-1,0.5,2,app=TRUE)
Phixy(1,-1,0.5,app=TRUE)
```

---

 rmse

*Root Mean Squared Error*


---

**Description**

Calculate the RMSE of an array of estimates relative to the true value.

**Usage**

```
rmse(rhohat, rho)
```

**Arguments**

rhohat	an array of estimators of rho.
rho	the true value of rho.



**Value**

the root mean squared error of rho-hat array.

**See Also**

[mb](#) [mrb](#)

**Examples**

```
rho = 0.5
rho-hat = 0.5 + rnorm(10)
rmse(rho-hat, rho)
```

---

summary\_MCCM\_est

*Summary a MCCM Estimation Result*

---

**Description**

Display the estimated correlation matrix and std matrix for a MCCM\_est list.

**Usage**

```
summary_MCCM_est(out_MCCM)
```

**Arguments**

out\_MCCM            output of function MCCM\_est.

**Value**

The summary of estimation.

**See Also**

[MCCM\\_est](#), [draw\\_correlation\\_matrix](#)

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